

Section – I

- 1.(b) Resultant of \vec{A} & \vec{B} lies on a plane and \vec{C} lies in another plane so resultant can never be zero.
- 2.(c) $P = \frac{W}{t}$
or, $t = \frac{W}{P} = \frac{mgh}{P}$
 $= \frac{200 \times 10 \times 40}{10 \times 10^3} = 8 \text{ sec}$
- 3.(b) When spring is cut in 4 equal parts then $K' = 4K$
 $\frac{T'}{T} = \sqrt{\frac{K}{K'}} = \sqrt{\frac{K}{4K}} = \frac{1}{2}$
 $\therefore T' = \frac{T}{2}$
- 4.(a) On heating upthrust decreases so it sink.
- 5.(a) $\frac{E'}{E} = \left(\frac{546}{273}\right)^4 = 16$
 $\therefore E' = 16E$
- 6.(a) $\omega t = 40t$ $kx = x$
or, $\omega = 40$ $k = 1$
or, $f = \frac{40}{2\pi}$ $\frac{2\pi}{\lambda} = 1$
 $\lambda = 2\pi$
 $\therefore v = f\lambda = \frac{40}{2\pi} \times 2\pi = 40 \text{ m/s}$
 $\therefore v = \sqrt{\frac{T}{m}}$
or, $T = v^2 m = 40^2 \times 10^{-2} = 16N$
- 7.(d) Distance = $30 + 10 + 10 = 50 \text{ cm}$
- 8.(c) Near point = -40 cm
 $u = 25 \text{ cm}$ $v = 40 \text{ cm}$
 $f = \frac{uv}{u+v} = \frac{25(-40)}{25-40} = +\frac{200}{15} \text{ cm} = \frac{2}{3} \text{ m}$
 $P = \frac{1}{f_{\text{min}}} = \frac{3}{2} = +1.5D$
- 9.(a) $V = \frac{W}{Q} = \frac{4}{20} = 0.2 \text{ V}$
- 10.(c) $I = \frac{E}{R+r} = \frac{50}{10+r}$
or, $10+r = \frac{50}{4.5} = 11.1$
 $\therefore r = 1.1 \Omega$
- 11.(a) When current divide in circle magnetic field at centre is zero.
- 12.(d) $T = 2\pi\sqrt{\frac{I}{MH}}$
 $I = \left(\frac{l^2 + b^2}{12}\right) m$, $M = 2\text{ml}$
Independent of length of suspension.
- 13.(b) $\frac{1}{\lambda} = R \left[\frac{1}{2^2} - \frac{1}{3^2} \right]$ for Hydrogen
or, $\frac{C}{\lambda} = CR \left[\frac{5}{36} \right]$
or, $f_0 = \frac{5RC}{36}$
For Helium $\frac{1}{\lambda} = Z^2 R \left[\frac{1}{2^2} - \frac{1}{3^2} \right]$

- or, $\frac{C}{\lambda} = Z^2 RC \left[\frac{5}{36} \right]$
or, $f' = 4RC \times \frac{5}{36} = 4f$
- 14.(b) Voltage gain = $\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{I_c R_{\text{out}}}{I_b R_{\text{in}}}$
 $= \beta \times \frac{24}{3}$
 $= 0.6 \times 8 = 4.8$
- 15.(d) $Mg > Al > Na$
Full filled s-orbital small site
- 16.(b) $-2 \times 2 + 3 \times 2$
 $N_2H_4 \rightarrow 2N$
Changes from -2 to $+3$ so that total of $10e$.
- 17.(b) $\Delta H = \Delta E + \Delta ngRT$ or $\Delta H = \Delta E + RT$ or $\Delta H > \Delta E$
- 18.(c) $H_2SO_4 \rightarrow H^+ + SO_4^{2-}$
 $H_2O \rightarrow H^+ + OH^-$
 $\downarrow \quad \downarrow$
 $H_2 \quad O_2$
cathode anode
- 19.(b) 20.(b) 21.(a) 22.(c) 23.(b) 24.(d)
25.(b) 26.(d) 27.(d) 28.(a)
- 29.(b) Here, $f(-x) = f(x) \rightarrow \text{even}$
 $f(-x) = -g(x) \rightarrow \text{odd}$
Now, $(f \circ g)(-x) = f(g(-x)) = f(-g(x)) = f(g(x)) = (f \circ g)(x)$
So, composite of even and odd functions is even.
 $A^2 - A + I = 0$ or $I = A - A^2$ or $I = A(I - A)$
 $\therefore A^{-1} = I - A$
- 31.(c) We have, $\text{Adj. } A = |A| I = 3 \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix} = \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$
- 32.(b) Given $x = 0 \rightarrow y\text{-axis}$
 $y = 0 \rightarrow x\text{-axis}$ and line $4x + 5y = 20$
Put $x = 0$, $y = 4$ which is y-intercept
Put $y = 0$ $x = 5$ which is x-intercept
Now, area of triangle = $\frac{1}{2} \times x\text{-intercept} \times y\text{-intercept}$
 $= \frac{1}{2} \times 5 \times 4 = 10 \text{ sq. units}$
- 33.(c) The circle is $x^2 + y^2 = 16$
Now, $5^2 + 4^2 - 16 = 25 > 0$. So the point (5, 4) is external and 2 tangents are possible.
- 34.(b) The parametric equations are
 $x = a \text{sech } t$, $y = b \tanh t$
Now, $\left(\frac{x}{a}\right)^2 + \left(\frac{y}{b}\right)^2 = \text{sech}^2 t + \tanh^2 t$
i.e., $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, which is an ellipse.
- 35.(d) Given conic section is $4x^2 - 9y^2 = 36$
i.e., $\frac{x^2}{9} - \frac{y^2}{4} = 1$ which is a hyperbola and $a = 3$, $b = 2$. So $|PS - PS'| = 2a = 2 \times 3 = 6$.
- 36.(c) Given equation is $x^2 + y^2 = 0$ which implies
 $x = 0$, $y = 0$
Here we can take any value of Z . So $(0, 0, Z)$ lies on Z -axis.
- 37.(b) Here, centroid of triangle $ABC = (2, 3, 4)$
So, coordinates of $A = (3 \times 2, 0, 0) = (6, 0, 0) \Rightarrow x\text{-intercept} = 6$

Coordinates of B = $(0 \times 3 \times 3, 0) = (0, 9, 0) \Rightarrow y$ -intercept = 9

Coordinates of C = $(0, 0, 3 \times 4) = (0, 0, 12) \Rightarrow z$ -intercept = 12

\therefore Required equation of plane is
 $\frac{x}{6} + \frac{y}{9} + \frac{z}{12} = 1$ or, $\frac{6x + 4y + 3z}{36} = 1$
i.e., $6x + 4y + 3z = 36$

38.(b) Here, $\vec{a} = \vec{i} + 2\vec{j} + 2\vec{k}$ So, $|\vec{a}| = \sqrt{1^2 + 2^2 + 2^2} = 3$
 $\vec{b} = 6\vec{i} - 2\vec{j} + 3\vec{k}$ So, $|\vec{b}| = \sqrt{6^2 + (-2)^2 + 3^2} = 7$

\therefore Projection of \vec{b} on $\vec{a} = \frac{|\vec{b}|}{|\vec{a}|} = \frac{7}{3}$
Projection of \vec{a} on \vec{b}

39.(c) Given $a = 1, b = 2, C = 60^\circ$
We have, area of $\triangle ABC = \frac{1}{2} \times ab \sin C$

$$= \frac{1}{2} \times 1 \times 2 \times \sin 60^\circ = \frac{\sqrt{3}}{2} \text{ sq. units}$$

40.(a) Regression equations are
 $20x - 9y - 107 = 0$ and $4x - 5y + 33 = 0$
The point of intersection (13, 17)
But point of intersection of regression lines
= (\bar{X}, \bar{Y})

$$\therefore \bar{X} = 13, \bar{Y} = 17$$

41.(b) Given $P(A \cap B) = \frac{1}{4} P(B)$. So $P(B) = 1 - P(B)$
 $= 1 - \frac{5}{8} = \frac{3}{8}$

$$\therefore P(A/B) = \frac{P(A \cap B)}{P(B)} = \frac{\frac{1}{4}}{\frac{3}{8}} = \frac{1}{4} \times \frac{8}{3} = \frac{2}{3}$$

42.(c) We have, $\sim(p \Rightarrow q) \equiv p \wedge (\sim q)$
So the negation of "If battery is low then mobile doesnot work well" is battery is low and mobile works well.

43.(c) To have unique solution of $AX = B$, A^{-1} must exists and for this we must have $|A| \neq 0$

44.(d) Here, $\lim_{x \rightarrow a^-} f(x) \neq \lim_{x \rightarrow a^+} f(x)$. So by definition the discontinuity is jump.

45.(a) $\lim_{n \rightarrow \infty} \frac{1 + 2 + 3 + \dots + n}{n^2}$
 $= \lim_{n \rightarrow \infty} \frac{n(n+1)}{2n^2}$
 $= \lim_{n \rightarrow \infty} \left(\frac{1}{2} + \frac{1}{n}\right) = \frac{1}{2} + 0 = \frac{1}{2}$

46.(c) Here, $\log_5 x = \log_5 e \log_e x$
So, $\frac{d \log_5 x}{dx} = \log_5 e \frac{d \log_e x}{dx} = \frac{\log_e 5}{x}$

47.(a) Suppose, $y = x^2$ So, $dy = 2x dx$
 $= 2 \times 2 \times 0.01 = 0.04$

48.(c) Given $\frac{dy}{dx} = ye^x$ or, $\frac{dy}{y} = e^x dx$

$$\text{Integrating } \int \frac{dy}{y} = \int e^x dx$$

$$\ln y = e^x + c$$

Using $y(0) = e$, we have $\ln e = e^0 + c \Rightarrow c = 0$

Then $\ln y = e^x$ So $\ln y = e^1 \therefore y = e^e$

49.(a) 50.(a) 51.(d) 52.(d) 53.(a) 54.(c)
55.(b) 56.(d) 57.(b) 58.(c) 59.(b) 60.(a)

Section - II

61.(c) PE of dart = Energy of spring

$$\text{or, } \frac{mgh_2}{mgh_1} = \left(\frac{x_2}{x_1}\right)^2 = \left(\frac{6}{4}\right)^2 = \frac{9}{4}$$

$$\therefore h_2 = \frac{9}{4} \times 2 = 4.5 \text{ m}$$

62.(a) $0 = \omega_0 + \alpha t$

$$\text{or, } \alpha = -\frac{\omega_0}{t} = -\frac{2\pi f}{10} = -\frac{2\pi \times 20}{10} = -4\pi \text{ rad/s}^2$$

$$\tau = I\alpha$$

$$= 5 \times 10^{-3} \times 4\pi = \frac{\pi}{50} \text{ N}$$

63.(a) Vol/s = Av

$$\text{or, } 70 \times 10^{-6} = 10^{-4} v$$

$$\text{or, } 70 \times 10^{-2} = \sqrt{2gh}$$

$$\text{or, } h = \frac{(70 \times 10^{-2})^2}{2g} = \frac{(70 \times 10^{-2})^2}{20}$$

$$= 0.0245 \text{ m}$$

$$= 2.45 \text{ cm}$$

64.(d) $T_2 V_2^{\gamma-1} = T_1 V_1^{\gamma-1}$

$$\text{or, } T_2 = 291 \left(\frac{V_1}{V_2}\right)^{1.4-1}$$

$$= 291(8)^{0.4} = 668 \text{ K}$$

$$= 395^\circ \text{C}$$

$$\therefore \Delta T = 395 - 18 = 377^\circ \text{C}$$

65.(b) $\frac{\text{gain in time in 1 day}}{\text{lose in time in 1 day}} = \frac{\frac{1}{2} \alpha (\theta - 16) \times 1 \text{ day}}{\frac{1}{2} \alpha (40 - \theta) \times 1 \text{ day}}$

$$\text{or, } \frac{5}{15} = \frac{(\theta - 16)}{(40 - \theta)}$$

$$\text{or, } 30 - 48 = 40 - \theta \quad \text{or, } \theta = \frac{88}{4} = 22^\circ \text{C}$$

66.(c) $\frac{v}{4l_{c1}} - \frac{v}{4l_{c2}} = 4$

$$\text{or, } \frac{v}{4} \left(\frac{1}{l_{c1}} - 1\right) = 4$$

$$\text{or, } \frac{1}{l_{c1}} = \frac{4 \times 4}{330} + 1 = \frac{346}{330}$$

$$\text{or, } l_{c1} = \frac{330}{346} = 0.95 \text{ m} = 95 \text{ cm}$$

67.(c) $\mu = \frac{\text{Real depth}}{\text{Apparent depth}}$

$$\frac{4}{3} = \frac{x}{21 - x}$$

$$84 - 4x = 3x$$

$$\text{or, } x = \frac{84}{7} = 12 \text{ cm}$$

68.(a) $d \sin \theta_1 = \lambda$

$$\text{or, } \sin \theta_1 = \frac{\lambda}{d}$$

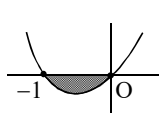
$$\text{or, } \theta_1 = \sin^{-1} \left(\frac{\lambda}{d}\right) = \sin^{-1} \left(\frac{6328 \times 10^{-10}}{6.2 \times 10^{-3}}\right) = 0.18^\circ$$

$$\therefore 2\theta_1 = 2 \times 0.18^\circ = 0.36^\circ$$

- 69.(b) $Q = (C_1 + C)V'$
or, $C_1V_1 = (C_1 + C)V'$
or, $C_1 + C = \frac{5 \times 10^{-6} \times 12}{3}$
or, $C = 20 \mu F - 5 \mu F = 15 \mu F$
- 70.(c) Deflection fall 50 div to 10 div means $I = 5I_g$
 $\therefore S = \frac{I_g G}{I - I_g}$ $G = \frac{12(5I_g - I_g)}{I_g} = 48\Omega$
- 71.(d) $E = \frac{d\phi}{dt} = AN \frac{dB}{dt}$
 $= (0.1)^2 \times 500 \times 1$
 $= 5V$
- 72.(b) 1st case
 $\frac{hc}{\lambda} = \phi + e \times 2.5V$
or, $ev = \left(\frac{hc}{\lambda} - \phi\right) \times \frac{1}{2.5} \dots (1)$
2nd case
 $\frac{hc}{1.5\lambda} = \phi + ev$
or, $ev = \left(\frac{hc}{1.5\lambda} - \phi\right) \dots (2)$
From (1) & (2)
 $\left(\frac{hc}{\lambda} - \phi\right) \frac{1}{2.5} = \frac{hc}{1.5\lambda} - \phi$
or, $\frac{hc}{2.5\lambda} - \frac{\phi}{2.5} = \frac{hc}{1.5\lambda} - \phi$
or, $\frac{hc}{1.5\lambda} - \frac{hc}{2.5\lambda} = \phi - \frac{\phi}{2.5}$
or, $\frac{hc}{\lambda} \left(\frac{1}{1.5} - \frac{1}{2.5}\right) = \frac{hc}{\lambda_0} \left(1 - \frac{1}{2.5}\right)$
or, $\lambda_0 = \frac{1.5 \times 2.5 \times 1.5}{2.5 \times 1} \lambda$
 $= 2.25\lambda$
- 73.(c) Initially
 $N_0 = \frac{6.023 \times 10^{23}}{99} \times 10^{-12}$
 $= 6.08 \times 10^9$
After 1 hr
 $N = N_0 \left(\frac{1}{2}\right)^{t/T_{1/2}}$
 $= 6.08 \times 10^9 \left(\frac{1}{2}\right)^{1/6} = 5.41 \times 10^9$
 $A = \lambda N = \frac{0.693}{T_{1/2}} \times N$
 $= \frac{0.693}{6} \times 5.41 \times 10^9 = 6.24 \times 10^8 \text{ dis/hr}$
- 74.(b) 5 moles of A need 10 moles of B
So B is limiting reagent
 \therefore 8 moles of B gives 4 moles C
- 75.(c)
- 76.(b) $V_a = ?$ $N_a = \frac{98 \times 1.8 \times 10}{49}$ $V_b = 200 \text{ ml}$ $N_b = 0.5N$
- 77.(c) Like CO_2 , SnS_2 is $[Sn^{++}]$ & $[S^{--}]^2$
- 78.(b) If concⁿ of A double rate also double so A is 1st order
& B is 2nd order.
- 79.(b) $Zn + NaOH \rightarrow Na_2ZnO_2 + H_2O$
excess amionic part
- 80.(d)

- 81.(c)
- $$\begin{array}{c} \text{O}^- \\ \parallel \\ \text{CH}_3 - \text{CH} + \text{HCN} \longrightarrow \text{CH}_3 - \text{CH} - \text{CN} \\ \uparrow \\ \text{OH} \end{array}$$
- Hydrolysis
- $$\begin{array}{c} \text{OH} \\ | \\ \text{CH}_3 - \text{CH} - \text{COOH} \\ \text{2-Hydroxy propanoic acid} \\ \text{or} \\ \text{(actic acid)} \end{array}$$
- 82.(d) $n(U) = 140$, $n(A) = 75$, $n(B) = 85$
Here maximum possible value of $n(A \cup B) = 140$
Minimum possible value of $n(A \cup B) = 85$
So, $n(A' \cap B') = n(A \cup B)' = n(U) - n(A \cup B)$
i.e., $n(A' \cap B') = 140 - n(A \cup B)$
 \therefore Maximum value of $n(A' \cap B') = 140 - 85 = 55$
Let a, b be two numbers. Then
 $a_1 A_1 A_2$, b are in A.P. So $A_1 - a = A_1 - A_2$
i.e., $A_1 + A_2 = a + b$
 a_1, G_1, G_2, b are in G.P. So $\frac{G_1}{a} = \frac{b}{G_2} \Rightarrow G_1 G_2 = ab$
and a_1, H_1, H_2, b are in H.P. So $\frac{1}{a}, \frac{1}{H_1}, \frac{1}{H_2}, \frac{1}{b}$ are in A.P.
Then, $\frac{1}{H_1} - \frac{1}{a} = \frac{1}{b} - \frac{1}{H_2} \Rightarrow \frac{1}{H_1} + \frac{1}{H_2} = \frac{1}{a} + \frac{1}{b} = \frac{a+b}{ab}$
or, $\frac{H_1 + H_2}{H_1 H_2} = \frac{a+b}{ab} = \frac{A_1 + A_2}{G_1 G_2}$
 $\therefore \frac{G_1 G_2}{H_1 H_2} = \frac{A_1 + A_2}{H_1 + H_2}$
- 83.(a) $\left(\frac{1+i}{1-i}\right)^x = 1$
or, $\left(\frac{1+i}{1-i} \times \frac{1+i}{1+i}\right)^x = 1$
or, $\left(\frac{1^2 + 2i + i^2}{1^2 - i^2}\right)^x = 1$
or, $\left(\frac{1 + 2i - 1}{1 + 1}\right)^x = 1$
or, $\left(\frac{2i}{2}\right)^x = 1$
or, $i^x = 1$
 $\therefore x = 4n, n \in \mathbb{Z}^+$
as $i^2 = -1$
- 84.(a)
- 85.(c) Given equation is
 $x^2 - |x| - 6 = 0$
When $x > 0$, the equation is $x^2 - x - 6 = 0$
i.e. $x = -2, 3$
 $\Rightarrow x = 3$
When $x < 0$ the equation, is $x^2 + x - 6 = 0$
i.e. $x = -3, 2 \Rightarrow x = -3$
 \therefore Product of real roots = $3 \times -3 = -9$
- 86.(c) Here, number of diagonals = 44
or, $\frac{n(n-3)}{2} = 44$
or, $n^2 - 3n = 88$
or, $n^2 - 3n - 88 = 0$
or, $n^2 - 11n + 8n - 88 = 0$

- or, $n(n-11) + 8(n-11) = 0$
or, $(n-11)(n+8) = 0$
 $\therefore n = 11$ or
 $n = -8$ (not possible)
- 87.(a)** We have $(1+x)^n = C_0 + C_1x + C_2x^2 + \dots + C_nx^n$
or, $x(1+x)^n = C_0x + C_1x^2 + C_2x^3 + \dots + C_nx^{n+1}$
Differentiating,
 $nx(1+x)^{n-1} + (1+x)^n = C_0 + 2C_1x + 3C_2x^2 + \dots + (n+1)C_nx^n$
Putting $x = 1$, we have
 $n2^{n-1} + 2^n = C_0 + 2C_1 + 3C_2 + \dots + (n+1)C_n$
 $\therefore (n+2)2^{n-1} = C_0 + 2C_1 + 3C_2 + \dots + (n+1)C_n$
- 88.(c)** Given equation $ax^2 + 2hxy + by^2 = 0$
Here, $m_1 + m_2 = -\frac{2h}{b}$, $m_1m_2 = \frac{a}{b}$
Suppose, $m_1 = m$, $m_2 = 2m$
Then, $m + 2m = -\frac{2h}{b}$, $m \cdot 2m = \frac{a}{b}$
or, $3m = -\frac{2h}{b}$ $2m^2 = \frac{a}{b}$
or, $m = -\frac{2h}{3b}$ $2 \times \left(-\frac{2h}{3b}\right)^2 = \frac{a}{b}$
or, $2 \cdot \frac{4h^2}{9b^2} = \frac{a}{b}$ $\therefore 8h^2 = 9ab$
- 89.(c)** Given line is $y = mx + c$ and parabola is $x^2 = 4ay$
Solving, $x^2 = 4a(mx + c)$
 $x^2 = 4amx + 4ac$
or, $x^2 - 4amx - 4ac = 0$
The line will touch if discriminant = 0
 $(-4am)^2 - 4 \times 1 \times (-4ac) = 0$
or, $16a^2m^2 + 16ac = 0 \Rightarrow c = -am^2$
- 90.(d)** Given $|\vec{a}| = 3$, $|\vec{b}| = 4$, $|\vec{c}| = 5$ and $\vec{a} + \vec{b} + \vec{c} = 0$
Now, $(\vec{a} + \vec{b} + \vec{c})^2 = |\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$
 $0 = 3^2 + 4^2 + 5^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$
or, $0 = 9 + 16 + 25 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$
or, $-50 = 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$
 $\therefore \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = -25$
- 91.(b)** $\sin^{-1}x + \sin^{-1}y = \frac{2\pi}{3}$ or, $\frac{\pi}{2} - \cos^{-1}x + \frac{\pi}{2} - \cos^{-1}y = \frac{2\pi}{3}$
i.e., $\cos^{-1}x + \cos^{-1}y = \frac{\pi}{3}$... (i)
and $\cos^{-1}x - \cos^{-1}y = \frac{\pi}{3}$... (ii)
Adding (i) and (ii),
 $2\cos^{-1}x = \frac{2\pi}{3} \Rightarrow \cos^{-1}x = \frac{\pi}{3} \Rightarrow x = \cos\frac{\pi}{3} = \frac{1}{2}$
From (i), $\frac{\pi}{3} + \cos^{-1}y = \frac{\pi}{3} \Rightarrow \cos^{-1}y = 0 \Rightarrow y = 1$
- 92.(c)** Given $\tan^{-1}\left(\frac{1+x}{1-x}\right) = \tan^{-1}\left(\frac{1+x}{1-x}\right) = \tan^{-1}(1) +$
 $\tan^{-1}x = \frac{\pi}{4} + \tan^{-1}x$

- So, $\frac{d}{dx} \tan^{-1}\left(\frac{1+x}{1-x}\right) = \frac{d}{dx} \frac{\pi/4}{1-x} + \frac{d}{dx} \frac{\tan^{-1}x}{1-x} = \frac{1}{1-x^2}$
- 93.(c)** Let x and y be two numbers whose sum is 4.
Then $x + y = 4$
i.e. $y = 4 - x$
Let $S = \frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{4}{x(4-x)} = \frac{4}{4x-x^2}$
Let $z = \frac{4x-x^2}{4}$
Then $\frac{dz}{dx} = \frac{4-2x}{4}$, $\frac{d^2z}{dx^2} = -\frac{1}{2}$
For maxima or minima, $\frac{dz}{dx} = 0 \Rightarrow \frac{4-2x}{4} = 0$
 $\Rightarrow x = 2$
and $\frac{d^2z}{dx^2} = -\frac{1}{2} < 0$
 $\therefore z$ is maximum and hence S is minimum.
So minimum value of $S = \frac{4}{4 \times 2 - 2^2} = \frac{4}{8-4} = \frac{4}{4} = 1$
- 94.(a)** Put $x = \tan\theta$ i.e. $dx = \sec^2\theta d\theta$
Then, $I = \int e^{\theta} \left(\frac{1 + \tan\theta + \tan^2\theta}{1 + \tan^2\theta} \right) \sec^2\theta d\theta$
 $= \int e^{\theta} \left(\frac{\tan\theta + \sec^2\theta}{\sec^2\theta} \right) \sec^2\theta d\theta$
 $= \int e^{\theta} (\tan\theta + \sec^2\theta) d\theta$
 $= e^{\theta} \tan\theta + c$
 $= e^{\tan^{-1}x} x + c$
- 95.(b)** Here $f(x) = x^2|x|$, $f(-x) = (-x)^2|-x| = x^2|x| = f(x)$
So, $\int_{-1}^1 x^2|x| dx$
 $= 2 \int_0^1 x^2|x| dx = 2 \int_0^1 x^2 x dx = 2 \int_0^1 x^3 dx$
 $= 2 \left[\frac{x^4}{4} \right]_0^1 = 2 \times \left(\frac{1}{4} - 0 \right) = \frac{1}{2}$
- 96.(c)** Given, $\frac{dy}{dx} = 2x + 1$
On integration,
 $\int dy = \int (2x + 1) dx$
 $y = x^2 + x + c$
But it passes through (1, 2).
So, $2 = 1^2 + 1 + c$
i.e. $c = 0$
So the curve is $y = x^2 + x$
Along x-axis, $y = 0$
 $x^2 + x = 0$
i.e. $x = 0, -1$
 \therefore Required area
 $= \int_{-1}^0 y dx = \int_{-1}^0 (x^2 + x) dx = \left[\frac{x^3}{3} + \frac{x^2}{2} \right]_{-1}^0$
 $= \frac{(-1)^3}{3} + \frac{(-1)^2}{2} = -\frac{1}{3} + \frac{1}{2} = \frac{-2+3}{6} = \frac{1}{6}$ sq. units
- 
- 97.(d)** **98.(a)** **99.(c)** **100.(d)**

...Best of Luck...