

**Section - I**

- 1.(a) Eq<sup>n</sup> when pendulum starts from extreme position, is  
 $y = A \cos \omega t$   
 or,  $\frac{A}{2} = A \cos\left(\frac{2\pi}{T} \times t\right)$   
 or,  $\cos\left(\frac{2\pi}{T} \times t\right) = \frac{1}{2} = \cos 60^\circ = \cos \frac{\pi}{3}$   
 or,  $\frac{2\pi}{T} t = \frac{\pi}{3} \quad t = \frac{T}{6}$
- 2.(b)
- 3.(b) % increase =  $\frac{\Delta l}{l} \times 100\%$   
 $= \alpha \Delta \theta \times 100\%$   
 $= 10^{-5} \times 100 \times 100\% = 0.1\%$
- 4.(a) Sudden compression  $\Rightarrow$  adiabatic process  
 $P_2 V_2^\gamma = P_1 V_1^\gamma$   
 or,  $P_2 \left(\frac{m}{d_2}\right)^\gamma = P_1 \left(\frac{m}{d_1}\right)^\gamma$   
 or,  $P_2 = P_1 \left(\frac{nd_1}{d_2}\right)^\gamma$  ( $\because d_2 = nd_1$ )  
 or,  $P_2 = n^\gamma P_1$
- 5.(c)  $S = \frac{dQ}{m \cdot d\theta}$   
 While boiling, temperature doesn't change, i.e.  $d\theta = 0$ ,  
 $\Rightarrow S = \infty$
- 6.(d) Sound wave is longitudinal wave which can't be polarized.
- 7.(d)  $\lambda_m = \frac{\lambda_v}{\mu}$   
 Since,  $\mu > 1$ ,  $\lambda_m < \lambda_v$ , i.e. wave length decreases but frequency is not affected.
- 8.(c) Two particles will have same velocity after a complete wave.
- 9.(a)  $\phi = \frac{Q}{\epsilon_0}$   
 Flux is independent to size but depends on charge so,  
 $\phi' = \frac{\phi}{2\epsilon_0} = \frac{\phi}{2}$
- 10.(d) When resistance is placed parallel with voltmeter then resistance decreases current increases so ammeter reading increases & voltmeter reading decreases.
- 11.(c) Breaking stress =  $\frac{F}{A}$   
 or,  $F = \text{Breaking stress} \times A$   
 or,  $F \propto A$   
 The load which can be supported by cable depends on area of cross-section remains constant.
- 12.(c)
- 13.(b) Semiconductor have -ve coefficient of resistance, so as temperature increases resistance decreases.
- 14.(b)  $nf = KE + \phi$   
 or,  $eV_s = hf - \phi$

- or,  $V_s = \frac{hf}{e} - \frac{\phi}{e}$   
 Which is in form,  $y = mx + c$   
 Where,  $m = \frac{h}{e}$
- 15.(b) Smaller the critical angle, more sparkling. Dipping diamond in water increases critical angle since refractive index decreases.
- 16.(b)  $E_C - E_A = E_C - E_B + E_B - E_A$   
 or,  $\frac{hc}{\lambda_3} = \frac{hc}{\lambda_1} + \frac{hc}{\lambda_2}$   
 $\Rightarrow \frac{1}{\lambda_3} = \frac{1}{\lambda_1} + \frac{1}{\lambda_2}$
- 17.(b)  $F = \frac{G(M-m)m}{R^2}$   
 F will be maximum if  $\frac{dF}{dm} = 0$   
 $M - 2m = 0$   
 $m = \frac{M}{2}$
- 18.(a) As halogens are most electronegative so configuration is  $ns^2 np^5$ .
- 19.(d)  $CO = 6+8=14$ ,  $O_2^{2+} = 16-2=14$ ,  $N_2 = 2 \times 7=14$ ,  $Si = 14$
- 20.(b) For M shell,  $n=3$ . Hence, no. of orbitals =  $n^2 = 3^2 = 9$
- 21.(c) In  $[Fe(H_2O)_5NO]$ ,  $NO^+ = 1$ ,  $H_2O = 0$ , so Fe has +1.
- 22.(c) Mass of water = 1 gm  
 Mole of water =  $\frac{1}{18}$   
 Molecules =  $\frac{1}{18} \times N_A = \frac{1}{18} \times 6.023 \times 10^{23} = 3.34 \times 10^{22}$
- 23.(a)  $H_2O + SO_2 \rightarrow H_2SO_3$  ( Sulphurous acid)
- 24.(b) ethyne
- 25.(c) 2-butyne ( $CH_3-C \equiv C-CH_3$ ) doesn't contain acidic H-atom so it doesn't give ppt with Tollen's reagent.
- 26.(a) In absence of peroxide electrophilic addition is observed. The first step is addition of  $H^+$  to alkene.
- 27.(a)
- 28.(b)
- 29.(b) Since,  $f(-x) = \frac{\sin^4(-x) + \cos^4(-x)}{-x + \tan(-x)}$   
 $= \frac{\sin^4(x) + \cos^4(x)}{-(x + \tan x)} = -f(x)$   
 $\Rightarrow f(x)$  is odd function.
- 30.(a)  $n(A \cup B) = n(A) + n(B) - n(A \cap B)$   
 $n(A \cup B)$  is maximum when  $n(A \cap B) = 0$   
 So,  $n(A \cup B) = n(A) + n(B) = 145 > n(U)$ , which is not possible.  
 So,  $[n(A \cup B)]_{\max} = 125$
- 31.(a)
- 32.(b)  $\sin^2 A + \sin^2 B = \sin^2 C$   
 $\Rightarrow \frac{a^2}{k^2} + \frac{b^2}{k^2} = \frac{c^2}{k^2}$   
 $\Rightarrow a^2 + b^2 = c^2$   
 $\Rightarrow \Delta$  is rt. angled at C
- 33.(a) Since, product of root =  $\frac{c}{a} = \frac{1}{1}$   
 $\Rightarrow \alpha \cdot \beta = 1 \quad \Rightarrow \beta = \frac{1}{\alpha}$

- 34.(d) Projection of  $\vec{a}$  on  $\vec{b} = a \cos \theta = |\vec{a}| \cos \theta$   
 Now,  $\vec{a} \cdot \vec{b} = |\vec{a}| |\vec{b}| \cos \theta$   
 or,  $|\vec{a}| \cos \theta = \frac{\vec{a} \cdot \vec{b}}{|\vec{b}|}$
- 35.(b) Area of  $\Delta$  made by line  $ax + by + c = 0$  with coordinate axis is  $\frac{c^2}{2|ab|}$   

$$= \frac{1 \cdot p^2}{2(\sin \alpha \cos \alpha)}$$

$$= \frac{p^2}{|\sin^2 \alpha|}$$
- 36.(b)  $x^2 + 5x + 6 = 0$   
 $\Rightarrow x = -2$   
 $x = -3$
- 37.(d) Pair of planes parallel to yz plane.  
 Length of L.R. = 4  $\times$  distance between vertex and focus  
 $= 4 \times 2a = 8a$
- 38.(c)  $\lim_{x \rightarrow \infty} \frac{x^{20}}{e^x}$   
 Using L' Hospital rule upto 20<sup>th</sup> time  
 $\lim_{x \rightarrow \infty} \frac{20!}{e^x} = \frac{20!}{\infty} = 0$
- 39.(d)  $\int_{-1}^1 x|x| dx = 0$  ( $\because x|x| = \text{odd function}$ )
- 40.(c)  $\sin^{-1}x + c$   
 (Derivative and anti-derivative are inverse of each other so they cancel each other)
- 41.(c)  $y = |x|$   
 or,  $\frac{dy}{dx} = \frac{x}{|x|}$  at  $x = 0$  is undefined.
- 42.(b)  $y = \sqrt{4 - x^2}$  represent upper half-part of circle  $x^2 + y^2 = 4$   
 So area =  $\frac{\pi \cdot 2^2}{2} = 2\pi$
- 43.(c)  $\cos^{-1}x + \cos^{-1}y \left( \frac{\pi}{2} - \sin^{-1}x \right) + \left( \frac{\pi}{2} - \sin^{-1}y \right)$   
 $= \pi - (\sin^{-1}x + \sin^{-1}y)$   
 $= \pi - \frac{\pi}{3} = \frac{2\pi}{3}$
- 44.(a)  $\sin^2x + \operatorname{cosec}^2x = 2$   
 or,  $\sin^2x + \frac{1}{\sin^2x} = 2$   
 or,  $\sin^4x - 2\sin^2x + 1 = 0$   
 or,  $(\sin^2x)^2 - 2 \cdot \sin^2x \cdot 1 + 1^2 = 0$   
 or,  $(\sin^2x - 1) = 0$   
 or,  $\sin^2x = 1$   
 $\Rightarrow x = n\pi \pm \frac{\pi}{2}$
- 45.(d)  $3x + 4y = 12$   
 $\Rightarrow \frac{x}{4} + \frac{y}{3} = 1$   
 So, portion intercepted =  $\sqrt{3^2 + 4^2} = 5$
- 46.(b) Sum of all coefficient =  $2^{10}$

- Sum of coefficient of even power of  $x = \frac{2^{10} + 2^9}{2} = 2^9$
- 47.(d)  $\frac{x}{a} = t + \frac{1}{t}, \frac{y}{b} = t - \frac{1}{t}$   
 or,  $\left(\frac{x}{a}\right)^2 - \left(\frac{y}{b}\right)^2 = \left(t + \frac{1}{t}\right)^2 - \left(t - \frac{1}{t}\right)^2$   
 or,  $\left(\frac{x}{a}\right)^2 - \left(\frac{y}{b}\right)^2 = 4$ , i.e. a hyperbola.
- 48.(b)  $\log_e e + \frac{\log_e 3}{1!} + \frac{(\log_e 3)^2}{2!} + \frac{(\log_e 3)^3}{3!} + \dots \infty$   
 $= e^{\log_e 3} = 3$
- 49.(d) 50.(c) 51.(a) 52.(b) 53.(a) 54.(c)  
 55.(a) 56.(a) 57.(d) 58.(d) 59.(c) 60.(a)

**Section - II**

- 61.(c) If a particle covers equal distance in 5<sup>th</sup> and 6<sup>th</sup> second, then during 5<sup>th</sup> second it moves up & during 6<sup>th</sup> second it moves down so, time to reach man height = 5s  
 $O = u - gt$   
 $u = 10 \times 5 = 50 \text{ m/s}$
- 62.(c) Loss in KE = Gain in PE  
 $\frac{1}{2}mv^2 + \frac{1}{2}I\omega^2 = mgh$   
 or,  $\frac{1}{2}mv^2 + \frac{1}{2}mk^2 \frac{v^2}{r^2} = mgh$   
 or,  $\frac{1}{2}mv^2 \left( 1 + \frac{k^2}{r^2} \right) = mgh$   

$$v^2 \left( \frac{k^2}{r^2} + 1 \right)$$
  
 or,  $h = \frac{2g}{2 \times 10} = \frac{10^2 \left( \frac{2r^2}{5r^2} + 1 \right)}{2 \times 10} = 7 \text{ m}$
- 63.(b)  $\omega = \omega_s - \omega_e$   
 $\Rightarrow \frac{2\pi}{T} = \frac{2\pi}{T_s} - \frac{2\pi}{T_e}$   
 $\Rightarrow \frac{1}{T} = \frac{1}{3} - \frac{1}{24}$   
 or,  $T = \frac{24}{7} \text{ hrs}$
- 64.(a)  $PV = RT$  for 1 mole  
 $W = \int PdV = \int \frac{RT}{V} dV$   
 Given,  $V = CT^{2/3}$   
 $\Rightarrow dV = C \cdot \frac{2}{3} T^{-1/3} dT$   
 $\frac{dV}{V} \Rightarrow \frac{2}{3} T^{-1} dT$   
 or,  $\frac{dV}{V} = \frac{2}{3} \frac{dT}{T}$   
 $W = \int_{T_1}^{T_2} RT \cdot \frac{2}{3} \frac{dT}{T}$   
 $= \frac{2}{3} R(T_2 - T_1)$   
 $= \frac{2R}{3} \times 30 = 20R$   
 $= 20 \times 8.31 = 166$

- 65.(b) Radiating power of black body,  
 $E = 6(T^4 - T_0^4) A$   
 $T_0 = 227^\circ\text{C} = 500 \text{ K}$ ,  
 $T_1 = 727^\circ\text{C} = 1000 \text{ K}$   
 $T_2 = 1227^\circ\text{C} = 1500 \text{ K}$   
 $E_1 = \sigma(1000^4 - 500^4) \dots$  (i)  
 $E_2 = \sigma(1500^4 - 500^4) \dots$  (ii)  
 Dividing,  $\frac{60}{E_2} = \frac{1000^4 - 500^4}{1500^4 - 500^4}$   $E_2 = 320 \text{ W}$
- 66.(c)  $\gamma = \alpha_1 + \alpha_2 + \alpha_3$   
 $= \alpha_1 + 2\alpha_2$
- 67.(a) The detector receives direct as well as reflected waves.  
 Distance moved between two consecutive position of maxima  $\frac{\lambda}{2}$   
 For 14 successive maxima  $= 14 \times \frac{\lambda}{2}$   
 Given,  $14 \times \frac{\lambda}{2} = 0.14$   
 or,  $\lambda = 2 \times 10^{-2} \text{ m}$   
 $\therefore f = \frac{c}{\lambda} = \frac{3 \times 10^8}{2 \times 10^{-2}} = 1.5 \times 10^{10} \text{ Hz}$
- 68.(b) The slope of image is  $m = \tan 135^\circ = -1$   
 Equation of line through origin,  $y = mx$   
 $y = -x$   
 $y + x = 0$
- 69.(a) Maxima is at P  
 $\frac{xd}{D} = n\lambda$   
 or,  $\frac{d}{2D} = n\lambda$   
 or,  $n = \frac{d^2}{2\lambda D}$
- 70.(d)  $\vec{E}_x = -\frac{\partial V}{\partial x} \hat{i} = -(2xy - z^2) \hat{i} = (2xy + z^2) \hat{i}$   
 $\vec{E}_y = -\frac{\partial V}{\partial y} \hat{j} = -(x^2) \hat{j} = x^2 \hat{j}$   
 $\vec{E}_z = -\frac{\partial V}{\partial z} \hat{k} = -(3xz^2) \hat{k} = 3xz^2 \hat{k}$   
 $\therefore \vec{E} = \vec{E}_x + \vec{E}_y + \vec{E}_z = (2xy + z^2) \hat{i} + x^2 \hat{j} + 3xz^2 \hat{k}$
- 71.(c)  $B_R = B_2 - B_1 = \frac{\mu_0 I_2}{2\pi \cdot \frac{r}{2}} - \frac{\mu_0 I_1}{2\pi \cdot \frac{r}{2}}$   
 $= \frac{\mu_0}{\pi \times 5} (5 - 2.5) = \frac{\mu_0}{2\pi}$
- 72.(d)  $E = -\frac{d\phi}{dt}$   
 $E = -\frac{d\phi}{dt}$   
 or,  $IR = -\frac{d}{dt}(6t^2 - 5t + 1)$   
 or,  $I = -\frac{(12t - 5)}{R}$   
 When  $t = 0.25 \text{ s}$   
 Then  $I = \frac{2}{10} = 0.2 \text{ A}$
- 73.(d)  $X^3 + Y^5 \rightarrow 2Z^4$   
 $\Delta E = [3 \times 5.3 + 5 \times 7.4] - 2(4 \times 6.2) = 3.3 \text{ MeV}$   
 Hence correct energy is option (d)
- 74.(b)  $\frac{N}{N_0} = \left(\frac{1}{2}\right)^n$ , n = no of decays  
 $\frac{1}{256} = \left(\frac{1}{2}\right)^n$   
 $\Rightarrow n = 8$  half lives  
 Times for 8 half lives  $= 8 \times 12.5 = 100 \text{ hrs}$
- 75.(a)  $M = \frac{E}{F} \times It$   
 or,  $500 = \frac{9}{96500} \times 25 \times t$   
 $t = 214444.4 \text{ sec} = 59.56 \text{ hrs}$
- 76.(c)  $N_{\text{mixture}} = \frac{300 \times 10^{-2} - 200 \times 10^{-3}}{300 + 200}$   
 $= 5.6 \times 10^{-3} \text{ N (w.r.t base)}$   
 $\text{pOH} = -\log(5.6 \times 10^{-3}) = 2.25$   
 $\text{pH} = 14 - 2.25 = 11.75$
- 77.(e)  $\text{C}_2\text{H}_5\text{Cl} + \text{Mg} \xrightarrow{\text{Dry Ether}} \text{C}_2\text{H}_5\text{MgCl} \xrightarrow{\text{H}_2\text{O}} \text{C}_2\text{H}_6 + \text{MgCl.OH}$
- 78.(a)  $K_C = \frac{[\text{PCO}]^2}{[\text{PCO}_2]} = \frac{8^2}{4} = 16 \text{ atm}$
- 79.(c) % of Haemoglobin = 0.33  
 wt of Iron  $= 67200 \times \frac{0.33}{100} = 221.76$   
 So, No. of Fe atoms  $= \frac{221.76}{56} = 3.96 \sim 4$
- 80.(d) No. of mole of  $\text{CO}_2 = \frac{88}{44} = 2$  mole  
 2 mole  $\text{CO}_2$  contain 4 mole oxygen atom.  
 1 mole  $\text{CO}$  contain 1 mole oxygen atom.  
 So, 4 mole  $\text{CO}$  contain 4 mole oxygen atom.  
 4 mole  $\text{CO} = 4 \times (12 + 16) = 112 \text{ gm}$
- 81.(a)  $\text{NaHSO}_3 + \text{NaHS} \rightarrow \text{Na}_2\text{S}_2\text{O}_3 + \text{H}_2\text{O}$   
 $\text{Na}_2\text{S}_2\text{O}_3 + \text{HCl} \rightarrow \text{NaCl} + \text{H}_2\text{O} + \text{SO}_2 + \text{S} \downarrow$   
colloidal
- 82.(d)  $\left| \frac{(3 + 4i)(\sin\theta + i\cos\theta)}{\sin\theta - i\cos\theta} \right|$   
 $= \frac{|3 + 4i| |\sin\theta + i\cos\theta|}{|\sin\theta - i\cos\theta|}$   
 $= \frac{(3^2 + 4^2) \cdot (1)}{(1)} = 5$
- 83.(c) For  $f(x)$  to be defined,  
 $|x| - x > 0$   
 or,  $x < |x|$ , which is true for all  $x \in (-\infty, 0)$
- 84.(b) Given equation can be written as  
 $5^{3x} + 45^x = 2.3^{3x}$   
 or,  $\left(\frac{5}{3}\right)^{3x} + \left(\frac{5}{3}\right)^x = 2$   
 Let,  $\left(\frac{5}{3}\right)^x = t$   
 $\Rightarrow t^3 + t - 2 = 0$   
 or,  $t^3 - 1 + t - 1 = 0$   
 or,  $(t - 1)(t^2 + t + 1) + (t - 1) = 0$   
 or,  $(t - 1)(t^2 + t + 2) = 0$   
 $\Rightarrow t = 1$   
 or,  $t^2 + t + 2 = 0$   
 But,  $t^2 + t + 2 = 0$  does not have real solutions  
 $\therefore t = 1$   
 $\Rightarrow \left(\frac{5}{3}\right)^x = 1 \Rightarrow x = 0$ , one solution only
- 85.(b)  $\frac{\cos A}{a} = \frac{\cos B}{b} = \frac{\cos C}{c}$   
 or,  $\frac{\cos A}{2R \sin A} = \frac{\cos B}{2R \sin B} = \frac{\cos C}{2R \sin C}$

- or,  $\cot A = \cot B = \cot C$   
 $\Rightarrow A = B = C$   
 $\Rightarrow \Delta$  is equilateral  
 $\therefore \text{Area} = \frac{\sqrt{3}}{4} l^2 = \frac{\sqrt{3}}{4} \times \frac{1}{6} = \frac{1}{8\sqrt{3}}$
- 86.(a) Given,  $\tan^{-1}(2x) + \tan^{-1}(3x) = \frac{\pi}{4}$   
 or,  $\tan^{-1}\left(\frac{2x+3x}{1-2x \cdot 3x}\right) = \tan^{-1}(1)$   
 or,  $\frac{5x}{1-6x^2} = 1$   
 or,  $6x^2 + 5x - 1 = 0 \quad x = \frac{1}{6}, -1$   
 But  $x = -1$  is in option
- 87.(c) Given,  $(1+x-2x^2)^6 = 1 + a_1x + a_2x^2 + \dots + a_{12}x^{12}$   
 Putting  $x = 1$ , we get  
 $0 = 1 + a_1 + a_2 + \dots + a_{12} \dots (1)$   
 Putting  $x = -1$ , we get  
 $64 = 1 - a_1 + a_2 - \dots + a_{12} \dots (2)$   
 Adding (1) & (2)  
 $64 = 2(1 + a_2 + a_4 + \dots)$   
 or,  $a_2 + a_4 + \dots + a_{12} = 31$
- 88.(c) Let  $\tan^{-1}x = y$   
 $\Rightarrow \frac{1}{1+x^2} dx = dy$  and  $x = \tan y$   
 $= \int e^y (1 + \tan y + \tan^2 y) dy$   
 $= \int e^y (\tan y + \sec^2 y) dy$   
 $= e^y \tan y + c$   
 $= e^{\tan^{-1}x} \cdot \tan(\tan^{-1}x) + c = e^{\tan^{-1}x} x + c$
- 89.(c) Since,  $(1-x)^{-1} = 1 + x + x^2 + \dots$   
 $\Rightarrow x = \frac{1}{1-a}, y = \frac{1}{1-b}, z = \frac{1}{1-c}$   
 Since,  $a, b, c$  are in A.P.  
 $\Rightarrow 1-a, 1-b, 1-c$  are in A.P.  
 $\Rightarrow \frac{1}{1-a}, \frac{1}{1-b}, \frac{1}{1-c}$  are in H.P.  
 $\Rightarrow x, y, z$  are in H.P.
- 90.(b)  $y = \tan^{-1}\left(\frac{5x-x}{1+5x \cdot x}\right) + \tan^{-1}\left(\frac{x+\frac{2}{3}}{1-\frac{2}{3}x}\right)$   
 or,  $y = \tan^{-1}(5x) - \tan^{-1}(x) + \tan^{-1}(x) + \tan^{-1}\left(\frac{2}{3}\right)$   
 or,  $y = \tan^{-1}(5x) + \tan^{-1}\left(\frac{2}{3}\right)$   
 or,  $\frac{dy}{dx} = \frac{5}{1+25x^2}$
- 91.(d) Area =  $\int_0^{\pi/4} \tan x dx + \int_{\pi/4}^{\pi/2} \cot x dx$   
 $= \log(\sec x) \Big|_0^{\pi/4} + \log(\sin x) \Big|_{\pi/4}^{\pi/2}$   
 $= \log\left(\frac{\sec \pi/4}{\sec 0}\right) + \log\left(\frac{\sin \pi/2}{\sin \pi/4}\right) = \log(\sqrt{2}) + \log\left(\frac{1}{\sqrt{2}}\right)$   
 $= \log\sqrt{2} + \log\sqrt{2}$

- $= 2\log\sqrt{2}$   
 $= \log 2$   
 So, answer are both a and b
- 92.(a)  $(\vec{a} + \vec{b}) \cdot \vec{b} = 0$   
 or,  $\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{b} = 0$   
 or,  $\vec{a} \cdot \vec{b} = -\vec{b} \cdot \vec{b} \dots (1)$   
 $(\vec{a} + 2\vec{b}) \cdot \vec{a} = 0$   
 or,  $\vec{a} \cdot \vec{a} + 2\vec{b} \cdot \vec{a} = 0$   
 or,  $\vec{a} \cdot \vec{a} + 2\vec{a} \cdot \vec{b} = 0$   
 or,  $\vec{a} \cdot \vec{a} - 2\vec{b} \cdot \vec{b} = 0$   
 or,  $|\vec{a}|^2 = 2|\vec{b}|^2$   
 or,  $|\vec{a}| = \sqrt{2}|\vec{b}|$
- 93.(c)  $y = (x^2 - 1)(x^2 - 5) = x^4 - 6x^2 + 5$   
 $\frac{dy}{dx} = 4x^3 - 12x$   
 $\frac{d^2y}{dx^2} = 12x^2 - 12$   
 For curve to be concave upwards  
 $f''(x) > 0$   
 i.e.  $12(x-1)(x+1) > 0$   
 or,  $(x-1)(x+1) > 0$   
 i.e.  $x < -1$  or  $x > 1$   
 $\Rightarrow |x| > 1$
- 94.(a) Given circle,  $(x-6)^2 + y^2 = 2$   
 Equation of tangent is,  $Y = mX + a\sqrt{1+m^2}$   
 Where  $Y = y, X = x-6$  for this question  
 or,  $y = m(x-6) + \sqrt{2}\sqrt{1+m^2}$   
 or,  $y = m(x-6) + \sqrt{2(1+m^2)}$   
 Focal point of  $y^2 = 16x$  is  $(a, 0) = (4, 0)$   
 Now, focal chord is tangent to circle, so focal point must satisfy equation of tangent so  
 $0 = m(4-6) + \sqrt{2(1+m^2)}$   
 or,  $2m = \sqrt{2(1+m^2)}$   
 or,  $4m^2 = 2 + 2m^2$   
 or,  $m^2 = 1$   
 or,  $m = \pm 1$
- 95.(c) On,  $y$ -axis,  $x = 0$  equation of circle becomes  
 $y^2 + y - 20 = 0$   
 $\Rightarrow y = -5 \text{ \& } 4$   
 So, circle touch  $y$  axis at  $(0, -5)$  &  $(0, 4)$   
 Hence, intercept length  $\Rightarrow |-5 - 4| = 9$
- 96.(c) Centroid,  $x = \frac{a \cos t + b \sin t + 1}{3}$   
 $\Rightarrow a \cos t + b \sin t = 3x - 1 \dots (1)$   
 $y = \frac{a \sin t - b \cos t}{3}$   
 $\Rightarrow a \sin t - b \cos t = 3y \dots (2)$   
 Squaring & adding (1) & (2)  
 $a^2 \cos^2 t + 2ab \cos t \sin t + b^2 \sin^2 t + a^2 \sin^2 t - 2ab \cos t \sin t + b^2 \cos^2 t$   
 $= (3x-1)^2 + (3y)^2$   
 or,  $a^2(\cos^2 t + \sin^2 t) + b^2(\sin^2 t + \cos^2 t) = (3x-1)^2 + (3y)^2$   
 or,  $(3x-1)^2 + (3y)^2 = a^2 + b^2$
- 97.(c) 98.(a) 99.(d) 100.(a)

...Best of Luck...