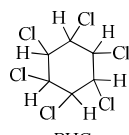


Section – I

- 1.(b) Resultant of $\vec{A}$ & $\vec{B}$ lies on a plane and $\vec{C}$ lies in another plane so resultant can never be zero.
- 2.(c) $P = \frac{W}{t}$
 or, $t = \frac{W}{P} = \frac{mgh}{P}$
 $= \frac{200 \times 10 \times 40}{10 \times 10^3} = 8 \text{ sec}$
- 3.(b) When spring is cut in 4 equal parts then $K' = 4K$
 $\frac{T'}{T} = \sqrt{\frac{K}{K'}} = \sqrt{\frac{K}{4K}} = \frac{1}{2}$
 $\therefore T' = \frac{T}{2}$
- 4.(a) On heating upthrust decreases so it sink.
- 5.(a) $\frac{E'}{E} = \left(\frac{546}{273}\right)^4 = 16$
 $\therefore E' = 16E$
- 6.(a) $\omega t = 40t$ $kx = x$
 or, $\omega = 40$ $k = 1$
 or, $f = \frac{40}{2\pi}$ $\frac{2\pi}{\lambda} = 1$
 $\lambda = 2\pi$
 $\therefore v = f\lambda = \frac{40}{2\pi} \times 2\pi = 40 \text{ m/s}$
 $\therefore v = \sqrt{\frac{T}{m}}$
 or, $T = v^2 m = 40^2 \times 10^{-2} = 16N$
- 7.(d) Distance = $30 + 10 + 10$
 $= 50 \text{ cm}$
- 8.(c) Near point = -40 cm
 $u = 25 \text{ cm}$ $v = 40 \text{ cm}$
 $f = \frac{uv}{u+v} = \frac{25(-40)}{25-40} = +\frac{200}{3} \text{ cm} = \frac{2}{3} \text{ m}$
 $P = \frac{1}{f_{\text{nm}}} = \frac{3}{2} = +1.5D$
- 9.(a) $V = \frac{W}{Q} = \frac{4}{20} = 0.2 \text{ V}$
- 10.(c) $I = \frac{E}{R+r} = \frac{50}{10+r}$
 or, $10+r = \frac{50}{4.5} = 11.1$
 $\therefore r = 1.1 \Omega$
- 11.(a) When current divide in circle magnetic field at centre is zero.

- 12.(d) $T = 2\pi\sqrt{\frac{I}{MH}}$
 $I = \left(\frac{l^2 + b^2}{12}\right) m$, $M = 2ml$
 Independent of length of suspension.
- 13.(b) $\frac{1}{\lambda} = R \left[\frac{1}{2^2} - \frac{1}{3^2} \right]$ for Hydrogen
 or, $\frac{C}{\lambda} = CR \left[\frac{5}{36} \right]$
 or, $f_0 = \frac{5RC}{36}$
 For Helium $\frac{1}{\lambda} = Z^2 R \left[\frac{1}{2^2} - \frac{1}{3^2} \right]$
 or, $\frac{C}{\lambda} = Z^2 RC \left[\frac{5}{36} \right]$
 or, $f' = 4RC \times \frac{5}{36} = 4f$
- 14.(b) Voltage gain = $\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{I_c R_{\text{out}}}{I_b R_{\text{in}}}$
 $= \beta \times \frac{24}{3}$
 $= 0.6 \times 8 = 4.8$
- 15.(a) No. of protons = No. of mole $\times N_A \times$ No. of protons in one molecule of CaCO_3
- 16.(b)
- 17.(b) MHPO_4 shows that valency of $M = 2$ (since HPO_4 has valency 2). Hence chloride will be MCl_2
- 18.(b)
- 19.(d)
- 20.(a)
- 21.(d) F^- is the most electronegative element.
- 22.(c) The impurity in extraction of copper is FeO which is removed by adding SiO_2 .
- 23.(d) It obeys Huckel's rule i.e. it contains $(4n+2)$ delocalized π electrons e.g. 10 π electrons.
- 

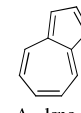
BHC



Cyclohexene



Cyclobutadiene



Azulene
- 24.(a) It is known as enyne compound. Its IUPAC format is: Alk-en-yne. Numbering is done by the lowest sum rule.
- 25.(d) Carbonium ion e.g. CH_3^+ (6 electrons)
 Free radical e.g. $\cdot\text{CH}_3$ (7 electrons)
 Nitrene e.g. CH_3N (6 electrons)
 Carbanion e.g. CH_3^- (8 electrons)

- 26.(d)** $(\text{CH}_3)_3\text{CNO}_2$, CCl_3CHO and $(\text{CH}_3)_3\text{CHO}$ do not have α hydrogen atoms so they do not show tautomerism.
- 27.(a)** +R or +M groups viz. $-\text{OH}$, OR , $-\text{NH}_2$, $-\text{X}$ etc give ortho and para substituted product due to mesomeric effect or resonating effect.
- 28.(c)**
- 29.(c)** We have $p \Rightarrow q \equiv (\sim q) \Rightarrow (\sim p)$
 So the equivalent statement must be if mobile works well then battery is not low.
- 30.(b)** $A - (A - B) = A \cap (A - B)' = A \cap (A \cap B)' = A \cap (A' \cup (B'))' = A \cap (A' \cup B) = (A \cap A') \cup (A \cap B) = A \cap B$
- 31.(c)** One root $= -2 + \sqrt{3}$
 As the irrational roots always occur in conjugate pair.
 So other root must be $-2 - \sqrt{3}$.
- 32.(d)** For equal roots, we must have, discriminant = 0
 $\Rightarrow (k+2)^2 - 4 \times 1.2k = 0$
 $\Rightarrow k^2 + 4k + 4 - 8k = 0$
 $\Rightarrow k^2 - 4k + 4 = 0$
 $\Rightarrow (k-2)^2 = 0$
 $\Rightarrow k = 2$
- 33.(a)** Here lines are parallel and have no point of intersection.
- 34.(c)** Here the lines $x = 0$ and $y = 0$ are perpendicular to each other. Hence the orthocentre = $(0, 0)$
- 35.(b)** Given $x^2 + y^2 = 0$ which is true only when $x^2 = 0, y^2 = 0$ i.e., $x = 0, y = 0$. So a point
- 36.(c)** Using fact that, product of parameters = -1 at the end of focal chord.
- 37.(d)** Given parabola is $y^2 = 2x$
 Here $a = \frac{1}{2}$
 and the line is $y = 2x + \lambda$.
 So $m = 2, c = \lambda$
 The line touches the parabola if
 $\lambda = am = \frac{1}{2} \times 2 = 1$
- 38.(a)** Distance from y-axis $= \sqrt{x^2 + z^2} = \sqrt{16 + 25} = \sqrt{41}$ units.
- 39.(c)** $\sqrt{6^2 + (-2)^2 + 3^2} = \sqrt{36 + 4 + 9} = \sqrt{49} = 7$
 So the direction cosines of a normal are
 $\frac{6}{7}, \frac{2}{7}, \frac{3}{7}$
- 40.(d)** Given $|\vec{a}| = 1, |\vec{b}| = 1, |\vec{a} + \vec{b}| = 1$, angle between $\vec{a}$ & $\vec{b} = \alpha$

- Now, $|\vec{a} + \vec{b}|^2 = 1$
 or, $|\vec{a}|^2 + |\vec{b}|^2 + 2\vec{a} \cdot \vec{b} = 1$
 or, $1 + 1 + 2|\vec{a}||\vec{b}|\cos\alpha = 1$
 or, $2.1.1\cos\alpha = -1$
 or, $\cos\alpha = -\frac{1}{2} \quad \therefore \alpha = 120^\circ$
- 41.(c)** $\sec^{-1}x = \text{cosec}^{-1}y$
 or, $\cos^{-1}\frac{1}{x} = \sin^{-1}\frac{1}{y}$
 or, $\cos^{-1}\frac{1}{x} = \frac{\pi}{2} - \cos^{-1}\frac{1}{y}$
 $\therefore \cos^{-1}\frac{1}{x} + \cos^{-1}\frac{1}{y} = \frac{\pi}{2}$
- 42.(d)** $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
 $= 0.4 + 0.5 - 0.12 = 0.78$
 $P(A \cap B) = 1 - P(A \cup B) = 1 - 0.78 = 0.22$
 $P(\bar{B}) = 1 - P(B) = 1 - 0.5 = 0.5$
 $\therefore P(\bar{A} \cap \bar{B}) = \frac{P(\bar{A} \cap \bar{B})}{P(\bar{B})} = \frac{P(A \cap B)}{P(B)} = \frac{0.22}{0.5} = 0.44$
- 43.(b)** Given $\sigma_x = 20, \sigma_y = 15, r = 0.48$
 $\therefore$ Regression coefficient of x on y $b_{xy} = r \frac{\sigma_x}{\sigma_y}$
 $= 0.48 \times \frac{20}{15} = 0.64$
- 44.(c)** Given $\lim_{x \rightarrow 0} \frac{\tan 2x - x}{3x - \sin x} = \lim_{x \rightarrow 0} \frac{\frac{\tan 2x}{2x} \times 2 - 1}{3 - \frac{\sin x}{x}}$
 $= \frac{2 - 1}{3 - 1} = \frac{1}{2}$
- 45.(c)** Since the function is continuous at $x = 0$.
 So we have $\lim_{x \rightarrow 0} f(x) = f(0)$
 or, $\lim_{x \rightarrow 0} x \sin \frac{1}{x} = k \quad \therefore k = 0$
- 46.(d)** Given $y = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots$ to ∞
 or, $y = -\left(-x - \frac{x^2}{2} - \frac{x^3}{3} - \dots\right)$ to ∞
 or, $y = -\ln(1 - x)$
 $\therefore \frac{dy}{dx} = \frac{1}{1 - x} - 1 = \frac{x}{1 - x}$
- 47.(b)** Given $f(x) = \tan^{-1}x$
 So $f'(x) = \frac{1}{1 + x^2} > 0$ for all real x
 $\therefore$ The function is strictly increasing.

48.(a) Given $y \sin x = x + c$

On differentiation, $y \frac{d \sin x}{dx} + \sin x \frac{dy}{dx} = \frac{dx}{dx} + \frac{dc}{dx}$

or, $\sin x \frac{dy}{dx} + y \cos x = 1$

or, $\frac{dy}{dx} + y \cot x = \operatorname{cosec} x$

On comparing with $\frac{dy}{dx} + Py = Q$ we get

$$Q = \operatorname{cosec} x$$

49.(a) 50.(a) 51.(d) 52.(d) 53.(a) 54.(c)

55.(b) 56.(d) 57.(b) 58.(c) 59.(b) 60.(a)

Section – II

61.(c) $\frac{h}{2} = \frac{g}{2} (2n - 1)$

or, $\frac{1}{2} \times \frac{1}{2} g n^2 = \frac{g}{2} (2n - 1)$

or, $n^2 - 4n + 2 = 0$

or, $n = 3.42 \text{ sec}$

$\therefore h = \frac{1}{2} g (3.42)^2$

$$= \frac{1}{2} \times 10 (3.42)^2$$

$$= 58 \text{ m}$$

62.(c) $\frac{Gm_1}{x^2} = \frac{Gm_2}{(1-x)^2} \Rightarrow x = \frac{1}{11} \text{ m}$

63.(b) Energy stored = K.E. of mass

$$\frac{1}{2} \frac{Y A e^2}{m l} = \frac{1}{2} m v^2$$

$$v = \sqrt{\frac{Y A e^2}{m l}} = \sqrt{\frac{5 \times 10^8 \times 10^{-6} \times 0.02^2}{5 \times 10^{-3} \times 0.1}} = 20 \text{ m/s}$$

64.(b) $E = \sigma A T^4 \times t = 4.45 \text{ kJ}$

65.(a) $(\mu - 1)t = n\lambda, \lambda = \frac{(\mu - 1)t}{n} = \frac{(1.5 - 1) \times 6 \times 10^{-6}}{5}$

$$= 6 \times 10^{-7} \text{ m} = 6000 \text{ \AA}$$

66.(b) $f_0 = \frac{1}{2L} \sqrt{\frac{\text{stress}}{\rho}} = \frac{1}{2l} \sqrt{\frac{Y \times \text{strain}}{\rho}} = 170 \text{ Hz}$

67.(c) $F = 9 \times 10^9 \cdot \frac{Q_1 Q_2}{r^2} \Rightarrow r^2 = 9 \times 10^9 \frac{Q_1 Q_2}{F} = 9 \text{ cm}$

68.(b) Amount of heat energy required for the water to boil

$$Q = 1 (100 - 20) \times 4200 + 420 \times 80 = 369600 \text{ J}$$

$$Q = 90\% \text{ of Pt, } t = 467 \text{ sec}$$

69.(d) $E = \frac{1}{2} m v^2$

$$v = \sqrt{\frac{2E}{m}} = \sqrt{\frac{2 \times 2 \times 10^6 \times 1.6 \times 10^{-19}}{1.67 \times 10^{-27}}}$$

$$= 1.96 \times 10^7 \text{ m/s}$$

$$F = Bev = 2.5 \times 1.6 \times 10^{-19} \times 1.96 \times 10^7$$

$$= 7.84 \times 10^{-12} \text{ N}$$

70.(c) $L = \frac{N\phi}{I} = 2.5 \times 10^{-3} \text{ H}$

The magnetic energy stored, $U = \frac{1}{2} LI^2 = 5 \times 10^{-3} \text{ J}$

71.(d) $\phi_0 = \frac{hc}{\lambda} - \text{K.E.} = 3 \times 10^{-19}$

$$f_0 = \frac{3 \times 10^{-19}}{h} = 4.5 \times 10^{14} \text{ Hz}$$

72.(d) For 1st member of Balmer series $\frac{1}{\lambda_B} = R \left(\frac{1}{4} - \frac{1}{9} \right)$

$$\Rightarrow \lambda_B = \frac{36}{5R}$$

For second member of same series,

$$\frac{1}{\lambda_B} = R \left(\frac{1}{4} - \frac{1}{16} \right) \Rightarrow \lambda_B = \frac{16}{3R} \dots (i)$$

i.e. $\frac{\lambda_B}{\lambda_B} = \frac{16 \times 5R}{3R \times 36}$

$$\therefore \lambda_B = \frac{20}{27} \times 6563 = 4861 \text{ \AA}$$

73.(b) $\frac{N'}{N_0}$

So, $\frac{N}{N_0} = 1 - \frac{N'}{N_0} = 1 - \frac{1}{4} = \frac{3}{4}$

$$\frac{N}{N_0} = \left(\frac{1}{2} \right)^{\frac{t}{T_{1/2}}}$$

or, $\frac{3}{4} = \left(\frac{1}{2} \right)^{\frac{t}{T_{1/2}}}$

$$\text{or, } \frac{\ln \left(\frac{3}{4} \right)}{\ln \left(\frac{1}{2} \right)} = \frac{t}{T_{1/2}}$$

or, $t = 224 \text{ yrs}$

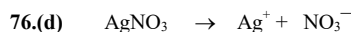
74.(c) New concentration of

$$\text{HCl} = \frac{10^{-6}}{100} = 10^{-8} \text{ M}$$

$$\therefore [\text{H}^+] = 10^{-8} + 10^{-7} = 1.1 \times 10^{-7} \text{ m}$$

$$\therefore \text{pH} \approx 6.95$$

75.(d) Find solubility by $4s^3 = K_{sp}$ for Ag_2S and $s^2 = K_{sp}$ for CuS and HgS



$$100 \text{ ml } 0.1 \text{ N} \qquad 100 \text{ ml } 0.1 \text{ N}$$

$$100 \text{ ml } 0.1 \text{ N} = 200 \text{ ml } \text{N}_2$$

$$\text{N}_2 = 0.05 \text{ N with respect to } \text{NO}_3^- \text{ ion.}$$

77.(c) 9 gram element $\rightarrow$ 8 gm O_2

So, eq. wt. of element is 9

At. wt. = $E \times v = 9 \times 3 = 27$

78.(a) Reaction whose rate is not affected by concentration or in which the concentration of the reactant do not change with time is called zero order reaction.

79.(a)

80.(c) $CH \equiv CH + HOCl \rightarrow CH(OH)_2 - CHCl_2 \xrightarrow{H_2O} CHOCHCl_2$

81.(a) The order of reactivity of alkyl halides towards elimination reaction follows the order: $3^\circ > 2^\circ > 1^\circ$.

82.(d) $n(U) = 140, n(A) = 75, n(B) = 85$

Here maximum possible value of $n(A \cup B) = 140$

Minimum possible value of $n(A \cup B) = 85$

So, $n(A' \cap B') = n(A \cup B)' = n(U) - n(A \cup B)$

i.e., $n(A' \cap B') = 140 - n(A \cup B)$

$\therefore$ Maximum value of $n(A' \cap B') = 140 - 85 = 55$

83.(a) Let a, b be two numbers. Then

$a_1 A_1 A_2, b$ are in A.P. So $A_1 - a = A_1 - A_2$

i.e., $A_1 + A_2 = a + b$

a_1, G_1, G_2, b are in G.P. So $\frac{G_1}{a} = \frac{b}{G_2} \Rightarrow G_1 G_2 = ab$

and a_1, H_1, H_2, b are in H.P. So $\frac{1}{a}, \frac{1}{H_1}, \frac{1}{H_2}, \frac{1}{b}$ are in A.P.

Then, $\frac{1}{H_1} - \frac{1}{a} = \frac{1}{b} - \frac{1}{H_2} \Rightarrow \frac{1}{H_1} + \frac{1}{H_2} = \frac{1}{a} + \frac{1}{b} = \frac{a+b}{ab}$

or, $\frac{H_1 + H_2}{H_1 H_2} = \frac{a+b}{ab} = \frac{A_1 + A_2}{G_1 G_2}$

$\therefore \frac{G_1 G_2}{H_1 H_2} = \frac{A_1 + A_2}{H_1 + H_2}$

84.(a) $\left(\frac{1+i}{1-i}\right)^x = 1$

or, $\left(\frac{1+i}{1-i} \times \frac{1+i}{1+i}\right)^x = 1$

or, $\left(\frac{1^2 + 2i + i^2}{1^2 - i^2}\right)^x = 1$

or, $\left(\frac{1+2i-1}{1+1}\right)^x = 1$

or, $\left(\frac{2i}{2}\right)^x = 1$

or, $i^x = 1$

$\therefore x = 4n, n \in \mathbb{Z}^+$

as $i^2 = -1$

85.(c) Given equation is

$$x^2 - |x| - 6 = 0$$

When $x > 0$, the equation is $x^2 - x - 6 = 0$

i.e. $x = -2, 3$

$\Rightarrow x = 3$

When $x < 0$ the equation, is $x^2 + x - 6 = 0$

i.e. $x = -3, 2 \Rightarrow x = -3$

$\therefore$ Product of real roots = $3 \times -3 = -9$

86.(c) Here, number of diagonals = 44

or, $\frac{n(n-3)}{2} = 44$

or, $n^2 - 3n = 88$

or, $n^2 - 3n - 88 = 0$

or, $n^2 - 11n + 8n - 88 = 0$

or, $n(n-11) + 8(n-11) = 0$

or, $(n-11)(n+8) = 0$

$\therefore n = 11$ or

$n = -8$ (not possible)

87.(a) We have $(1+x)^n = C_0 + C_1 x + C_2 x^2 + \dots + C_n x^n$

or, $x(1+x)^n = C_0 x + C_1 x^2 + C_2 x^3 + \dots + C_n x^{n+1}$

Differentiating,

$nx(1+x)^{n-1} + (1+x)^n = C_0 + 2C_1 x + 3C_2 x^2 + \dots + (n+1)C_n x^n$

Putting $x = 1$, we have

$n2^{n-1} + 2^n = C_0 + 2C_1 + 3C_2 + \dots + (n+1)C_n$

$\therefore (n+2)2^{n-1} = C_0 + 2C_1 + 3C_2 + \dots + (n+1)C_n$

88.(c) Given equation $ax^2 + 2hxy + by^2 = 0$

Here, $m_1 + m_2 = -\frac{2h}{b}, m_1 m_2 = \frac{a}{b}$

Suppose, $m_1 = m, m_2 = 2m$

Then, $m + 2m = -\frac{2h}{b}, m \cdot 2m = \frac{a}{b}$

or, $3m = -\frac{2h}{b}, 2m^2 = \frac{a}{b}$

or, $m = -\frac{2h}{3b}, 2 \times \left(-\frac{2h}{3b}\right)^2 = \frac{a}{b}$

or, $2 \frac{4h^2}{9b^2} = \frac{a}{b} \therefore 8h^2 = 9ab$

89.(c) Given line is $y = mx + c$ and parabola is $x^2 = 4ay$

Solving, $x^2 = 4a(mx + c)$

$$x^2 = 4amx + 4ac$$

or, $x^2 - 4amx - 4ac = 0$

The line will touch if discriminant = 0

$$(-4am)^2 - 4 \times 1 \times -4ac = 0$$

or, $16a^2 m^2 + 16ac = 0 \Rightarrow c = -am^2$

90.(d) Given $|\vec{a}| = 3, |\vec{b}| = 4, |\vec{c}| = 5$ and $\vec{a} + \vec{b} + \vec{c} = 0$

Now, $(\vec{a} + \vec{b} + \vec{c})^2 = |\vec{a}|^2 + |\vec{b}|^2 + |\vec{c}|^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$

$$0 = 3^2 + 4^2 + 5^2 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$$

or, $0 = 9 + 16 + 25 + 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$

or, $-50 = 2(\vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a})$

$\therefore \vec{a} \cdot \vec{b} + \vec{b} \cdot \vec{c} + \vec{c} \cdot \vec{a} = -25$

91.(b) $\sin^{-1}x + \sin^{-1}y = \frac{2\pi}{3}$ or, $\frac{\pi}{2} - \cos^{-1}x + \frac{\pi}{2} - \cos^{-1}y = \frac{2\pi}{3}$

i.e., $\cos^{-1}x + \cos^{-1}y = \frac{\pi}{3}$... (i)

and $\cos^{-1}x - \cos^{-1}y = \frac{\pi}{3}$... (ii)

Adding (i) and (ii),

$$2\cos^{-1}x = \frac{2\pi}{3} \Rightarrow \cos^{-1}x = \frac{\pi}{3} \Rightarrow x = \cos\frac{\pi}{3} = \frac{1}{2}$$

From (i), $\frac{\pi}{3} + \cos^{-1}y = \frac{\pi}{3} \Rightarrow \cos^{-1}y = 0 \Rightarrow y = 1$

92.(c) Given $\tan^{-1}\left(\frac{1+x}{1-x}\right) = \tan^{-1}\left(\frac{1+x}{1-x}\right) = \tan^{-1}(1) + \tan^{-1}x = \frac{\pi}{4} + \tan^{-1}x$

So, $\frac{d}{dx} \tan^{-1}\left(\frac{1+x}{1-x}\right) = \frac{d}{dx} \frac{\pi/4}{1} + \frac{d}{dx} \tan^{-1}x = \frac{1}{1+x^2}$

93.(c) Let x and y be two numbers whose sum is 4.

Then $x + y = 4$

i.e. $y = 4 - x$

Let $S = \frac{1}{x} + \frac{1}{y} = \frac{x+y}{xy} = \frac{4}{x(4-x)} = \frac{4}{4x-x^2}$

Let $z = \frac{4x-x^2}{4}$

Then $\frac{dz}{dx} = \frac{4-2x}{4}$, $\frac{d^2z}{dx^2} = -\frac{1}{2}$

For maxima or minima, $\frac{dz}{dx} = 0 \Rightarrow \frac{4-2x}{4} = 0$

$$\Rightarrow x = 2$$

and $\frac{d^2z}{dx^2} = -\frac{1}{2} < 0$

$\therefore z$ is maximum and hence S is minimum.

So minimum value of $S = \frac{4}{4 \times 2 - 2^2} = \frac{4}{8-4} = \frac{4}{4} = 1$

94.(a) Put $x = \tan\theta$ i.e. $dx = \sec^2\theta d\theta$

Then, $I = \int e^{\theta} \left(\frac{1 + \tan\theta + \tan^2\theta}{1 + \tan^2\theta} \right) \sec^2\theta d\theta$

$$= \int e^{\theta} \left(\frac{\tan\theta + \sec^2\theta}{\sec^2\theta} \right) \sec^2\theta d\theta$$

$$= \int e^{\theta} (\tan\theta + \sec^2\theta) d\theta$$

$$= e^{\theta} \tan\theta + c$$

$$= e^{\tan^{-1}x} x + c$$

95.(b) Here $f(x) = x^2|x|$, $f(-x) = (-x)^2|-x| = x^2|x| = f(x)$

So, $\int_{-1}^1 x^2|x| dx$

$$= 2 \int_0^1 x^2|x| dx = 2 \int_0^1 x^2 x dx = 2 \int_0^1 x^3 dx$$

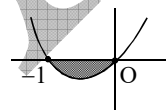
$$= 2 \left[\frac{x^4}{4} \right]_0^1 = 2 \times \left(\frac{1}{4} - 0 \right) = \frac{1}{2}$$

96.(c) Given, $\frac{dy}{dx} = 2x + 1$

On integration,

$$\int dy = \int (2x + 1) dx$$

$$y = x^2 + x + c$$



But it passes through (1, 2).

So, $2 = 1^2 + 1 + c$

i.e. $c = 0$

So the curve is $y = x^2 + x$

Along x-axis, $y = 0$

$$x^2 + x = 0$$

i.e. $x = 0, -1$

$\therefore$ Required area

$$= \int_0^{-1} y dx = \int_0^{-1} (x^2 + x) dx = \left[\frac{x^3}{3} + \frac{x^2}{2} \right]_0^{-1}$$

$$= \frac{(-1)^3}{3} + \frac{(-1)^2}{2} = -\frac{1}{3} + \frac{1}{2} = \frac{-2+3}{6} = \frac{1}{6} \text{ sq. units}$$

97.(c)

98.(b)

99.(c)

100.(d)

...The End...