

2082-10-10 Hints & Solution

Section - I

- 1.(d) $R = \frac{2u_x u_y}{g} = \frac{2 \times 5 \times 4}{10} = 4\text{m}$
- 2.(a) Energy density $= \frac{1}{2} \times \text{Stress} \times \text{Strain}$
 $= \frac{1}{2} \times (Y \times \text{Strain}) \times \text{Strain}$
 $= \frac{1}{2} Y \alpha^2$
- 3.(d) $\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$
 or, $\frac{1}{\frac{\rho_{eq} l}{2A}} = \frac{1}{\frac{\rho_1 l}{A}} + \frac{1}{\frac{\rho_2 l}{A}}$
 or, $\frac{2}{\rho_{eq}} = \frac{1}{\rho_1} + \frac{1}{\rho_2}$
 or, $\rho_{eq} = \frac{2\rho_1\rho_2}{\rho_1 + \rho_2}$
- 4.(c) $\beta = \frac{\alpha}{1-\alpha} = \frac{0.9}{1-0.9} = 9$
- 5.(d) $\frac{R}{R_{Fe}} = \left(\frac{A}{56}\right)^{1/3} \left\{ \because R \propto A^{1/3} \right\}$
 $\frac{1}{2} R_{Fe} = \left\{ \frac{A}{56} \right\}^{1/3} \left\{ \because R = \frac{1}{2} R_{Fe} \right\}$
 or, $\frac{1}{8} = \frac{A}{56}$
 or, $A = 7$
- 6.(b) $F_{medium} = \frac{\mu_r \mu_0 I_1 I_2}{2\pi r}$
 $= \mu_r \times F_{vacuum}$
 $= 10 \times 2 \times 10^{-7}$
 $= 2 \times 10^{-6} \text{ N/m}$
- 7.(c) K.E. per molecule $= \frac{3}{2} KT$; $T = \text{constant}$.
- 8.(d) For 1st overtone
 $\frac{\lambda}{2} + \frac{\lambda}{2} = l$ or, $\lambda = l$
- 9.(c) Induced charge $= \frac{\Delta\phi}{R}$; $\Delta\phi = \text{change of flux}$
 $R = \text{resistance}$
- 10.(c) $y = \frac{1}{2} \frac{qE}{m} \frac{x^2}{v^2}$
 or, $y = \frac{qEx^2}{4KE} \left(\because KE = \frac{1}{2} mv^2 \right)$
 i.e. $y \propto q$ (change)
 Charge of $\alpha >$ change of proton = change of electron.
- 11.(b) The potential inside conductor is same as that on surface as inside conductor is equipotential surface.
- 12.(b) At height h ,
 $P.E = \frac{1}{3} K.E$
 $\Rightarrow K.E = 3P.E$
 $\therefore \text{Total energy (E)} = K.E + P.E$
 $= 4P.E$
 Now, $4P.E = \frac{1}{2} \mu u^2 \left(\because \frac{1}{2} \mu u^2 \text{ is initial total energy} \right)$
 or, $4 \times mgh = \frac{1}{2} \mu u^2$ or, $h = \frac{u^2}{8g}$

- 13.(a) $P = IV$
 $= \frac{ne}{t} \times v$
- 14.(c) $I = I_0 \cos^2 \theta$
 or, 25% of $I_0 = I_0 \cos^2 \theta$
 or, $\cos \theta = \frac{1}{2}$
 $\therefore \theta = 60$
- 15.(c) 16.(b) 17.(b) 18.(a) 19.(b)
 20.(a) 21.(b) 22.(c) 23.(b) 24.(b)
 25.(c) 26.(d) 27.(d) 28.(b)
- 29.(c) We have $p \Rightarrow q \equiv (\sim q) \Rightarrow (\sim p)$
 So the equivalent statement must be if mobile works well then battery is not low.
- 30.(b) $A - (A - B) = A \cap (A - B)' = A \cap (A \cap B)' = A \cap (A' \cup (B'))' = A \cap (A' \cup B)$
 $= (A \cap A') \cup (A \cap B) = A \cap B$
- 31.(c) One root $= -2 + \sqrt{3}$
 As the irrational roots always occur in conjugate pair.
 So other root must be $-2 - \sqrt{3}$.
- 32.(d) For equal roots, we must have, discriminant $= 0$
 $\Rightarrow (k+2)^2 - 4 \times 1.2k = 0$
 $\Rightarrow k^2 + 4k + 4 - 8k = 0$
 $\Rightarrow k^2 - 4k + 4 = 0$
 $\Rightarrow (k-2)^2 = 0$
 $\Rightarrow k = 2$
- 33.(a) Here lines are parallel and have no point of intersection.
- 34.(c) Here the lines $x = 0$ and $y = 0$ are perpendicular to each other. Hence the orthocentre $= (0, 0)$
- 35.(b) Given $x^2 + y^2 = 0$ which is true only when
 $x^2 = 0, y^2 = 0$ i.e., $x = 0, y = 0$. So a point
- 36.(c) Using fact that, product of parameters $= -1$ at the end of focal chord.
- 37.(d) Given parabola is $y^2 = 2x$
 Here $a = \frac{1}{2}$
 and the line is $y = 2x + \lambda$.
 So $m = 2, c = \lambda$
 The line touches the parabola if
 $\lambda = am = \frac{1}{2} \times 2 = 1$
- 38.(a) Distance from y-axis $= \sqrt{x^2 + z^2} = \sqrt{16 + 25} = \sqrt{41}$ units.
- 39.(c) $\sqrt{6^2 + (-2)^2 + 3^2} = \sqrt{36 + 4 + 9} = \sqrt{49} = 7$
 So the direction cosines of a normal are
 $\frac{6}{7}, \frac{-2}{7}, \frac{3}{7}$
- 40.(d) Given $|\vec{a}| = 1, |\vec{b}| = 1, |\vec{a} + \vec{b}| = 1$, angle between \vec{a} & $\vec{b} = \alpha$
 Now, $|\vec{a} + \vec{b}|^2 = 1$
 or, $|\vec{a}|^2 + |\vec{b}|^2 + 2\vec{a} \cdot \vec{b} = 1$
 or, $1 + 1 + 2|\vec{a}||\vec{b}|\cos\alpha = 1$
 or, $2.1.1 \cos\alpha = -1$
 or, $\cos\alpha = -\frac{1}{2} \therefore \alpha = 120^\circ$

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- 41.(c) $\sec^{-1}x = \operatorname{cosec}^{-1}y$
 or, $\cos^{-1}\frac{1}{x} = \sin^{-1}\frac{1}{y}$
 or, $\cos^{-1}\frac{1}{x} = \frac{\pi}{2} - \cos^{-1}\frac{1}{y}$
 $\therefore \cos^{-1}\frac{1}{x} + \cos^{-1}\frac{1}{y} = \frac{\pi}{2}$
- 42.(d) $P(A \cup B) = P(A) + P(B) - P(A \cap B)$
 $= 0.4 + 0.5 - 0.12 = 0.78$
 $P(A \cup B) = 1 - P(A \cap B) = 1 - 0.78 = 0.22$
 $P(B) = 1 - P(A) = 1 - 0.5 = 0.5$
 $\therefore P(\bar{A}/B) = \frac{P(\bar{A} \cap B)}{P(B)} = \frac{P(A \cup B)}{P(B)} = \frac{0.22}{0.5} = 0.44$
- 43.(b) Given $\sigma_x = 20$ $\sigma_y = 15$ $r = 0.48$
 \therefore Regression coefficient of x on y $b_{xy} = r \frac{\sigma_x}{\sigma_y}$
 $= 0.48 \times \frac{20}{15} = 0.64$
- 44.(c) Given $\lim_{x \rightarrow 0} \frac{\tan 2x - x}{3x - \sin x} = \lim_{x \rightarrow 0} \frac{\frac{\tan 2x}{2x} \times 2 - 1}{3 - \frac{\sin x}{x}}$
 $= \frac{2 - 1}{3 - 1} = \frac{1}{2}$
- 45.(c) Since the function is continuous at $x = 0$.
 So we have $\lim_{x \rightarrow 0} f(x) = f(0)$
 or, $\lim_{x \rightarrow 0} x \sin \frac{1}{x} = k \quad \therefore k = 0$
- 46.(d) Given $y = x + \frac{x^2}{2} + \frac{x^3}{3} + \dots$ to ∞
 or, $y = -\left(-x - \frac{x^2}{2} - \frac{x^3}{3} - \dots \text{ to } \infty\right)$
 or, $y = -\ln(1 - x)$
 $\therefore \frac{dy}{dx} = \frac{1}{1 - x} - 1 = \frac{x}{1 - x}$
- 47.(b) Given $f(x) = \tan^{-1}x$
 So $f'(x) = \frac{1}{1 + x^2} > 0$ for all real x
 \therefore The function is strictly increasing.
- 48.(a) Given $y \sin x = x + c$
 On differentiation, $y \frac{d \sin x}{dx} + \sin x \frac{dy}{dx} = \frac{dx}{dx} + \frac{dc}{dx}$
 or, $\sin x \frac{dy}{dx} + y \cos x = 1$
 or, $\frac{dy}{dx} + y \cot x = \operatorname{cosec} x$
 On comparing with $\frac{dy}{dx} + Py = Q$ we get
 $Q = \operatorname{cosec} x$
- 49.(b) 50.(b) 51.(d) 52.(d) 53.(c) 54.(c)
 55.(d) 56.(d) 57.(b) 58.(b) 59.(c) 60.(a)

Section - II

- 61.(c) $I_{CD} = I_{AB} + Md^2$ (Parallel axis theorem)
 or, $mk_{CM}^2 + Md^2$
 or, $K_{CM} = \sqrt{K^2 - d^2}$
 or, $K_{CM} = \sqrt{10^2 - 6^2} = 8 \text{ cm}$

- 62.(c) $3mv = \sqrt{(m \times 39)^2 + (m \times 39)^2}$
 or, $v = \frac{\sqrt{2 \times 39^2}}{3}$
 or, $v = 13\sqrt{2} \text{ m/s}$
- 63.(b) $E = K \frac{l}{3} = \frac{V}{l} \times \frac{l}{3} \dots (1) \quad \left(\because K = \frac{V}{l}\right)$
 $E = K'l' = \frac{V}{l + \frac{l}{2}} \times l' \dots (2)$
 From (1) and (2)
 $\frac{V}{l} \times \frac{l}{3} = \frac{V}{\frac{3l}{2}} \times l'$
 or, $l' = \frac{l}{2}$
- 64.(b) $I \propto f^2 a^2$
 $\therefore \frac{I_1}{I_2} = \left(\frac{f_1}{f_2}\right)^2 \times \left(\frac{a_1}{a_2}\right)^2$
 or, $\frac{1}{36} = \left(\frac{1}{2}\right)^2 \times \left(\frac{a_1}{a_2}\right)^2$
 or, $\frac{a_1}{a_2} = \frac{1}{3}$
 65.(b) $\frac{m}{m_0} = \left(\frac{1}{2}\right)^{vT_{1/2}}$
 or, $80\% = \left(\frac{1}{2}\right)^{vT_{1/2}}$
 or, $0.8 = (0.5)^{vT_{1/2}}$
 or, $T_{1/2} = 31 \text{ days}$
 Again $\frac{m'}{m_0} = \left(\frac{1}{2}\right)^{vT_{1/2}} \times 100\%$
 $= \left(\frac{1}{2}\right)^{20/31} \times 100\%$
 $= 63.9\%$
- 66.(a) $\frac{hc}{\lambda} = E_{ion} + K.E.$
 or, $\lambda = \frac{hc}{E_{ion} + K.E.}$
 or, $\lambda = \frac{6.62 \times 10^{-34} \times 3 \times 10^8}{(13.6 + 2.4) \times 1.6 \times 10^{-19}}$
 or, $\lambda = 7.75 \times 10^{-8} \text{ m}$
- 67.(d) $Q = 6 - 2 = 4 \mu C$
 $\therefore Q_1 = Q_2 = \frac{Q}{2} = 2 \mu C = 2 \times 10^{-6} C$
 Then, $F = \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2}$
 $= \frac{9 \times 10^9 \times 2 \times 10^{-6} \times 2 \times 10^{-6}}{(0.2)^2}$
 $= 0.9 \text{ N}$
- 68.(b) $S = \frac{G}{n - 1}; n = \frac{I}{I_g} = 6$
 $= \frac{10}{6 - 1}$
 $= 2 \Omega$ in parallel
- 69.(c) $h = \frac{2T \cos \theta}{r \rho g}$
 or, $\frac{h}{\cos \theta} = \frac{2T}{r \rho g} = \text{constant}$
 $\therefore \frac{h_1}{\cos \theta_1} = \frac{h_2}{\cos \theta_2}$

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- or, $\cos\theta_2 = \frac{h_2}{h_1} \times \cos\theta_1$
 or, $\cos\theta_2 = \frac{1}{2} \times \cos 0^\circ$
 or, $\theta_2 = 60^\circ$
70.(a) For maxima,
 path diff = $n\lambda$
 or, $\frac{y_d}{D} = n\lambda$
 or, $\frac{d}{2} \times \frac{d}{D} = n\lambda \left(\because y = \frac{d}{2} \right)$

$$n = \frac{d^2}{2\lambda D}$$
- 71.(d)** $T_1 V_1^{1-\gamma} = T_2 V_2^{1-\gamma}$ ($\because TV^{1-\gamma} = \text{constant}$)
 or, $T_2 = T_1 \times \left(\frac{V_1}{V_2} \right)^{\gamma-1}$
 or, $T_2 = 300 \times \left(\frac{V_1}{\frac{1}{4} V_1} \right)^{1.4-1}$
 or, $T_2 = 300 \times 4^{0.4} = 522.3 \text{ K}$
- 72.(b)** $\cos\theta = \frac{R}{Z} = \frac{R}{\sqrt{R^2 + X^2}}$
 or, $\cos\theta = \frac{3}{\sqrt{3^2 + 4^2}}$
 or, $\cos\theta = 0.6$
- 73.(a)** $dQ = msdT = m \times \frac{1}{2} T^2 dT \left(\because S = \frac{1}{2} T^2 \right)$

$$\therefore Q = \int_0^{50} dQ$$
 or, $Q = \frac{m}{2} \int_0^{50} T^2 dT$
 or, $Q = \frac{m}{2} \times \left[\frac{T^3}{3} \right]_0^{50}$
 or, $Q = \frac{2}{2} \times \frac{1}{3} \times 50^3$

$$= 41666 \text{ J}$$
- 74.(b)** Molar mass of $\text{MgSO}_4 = 24 + 32 + (16 \times 4) = 120 \text{ g/mol}$
 Moles = $9.6/120 = 0.08 \text{ mol}$
- 75.(c)** Rate $\propto [\text{N}_2][\text{H}_2]^3$. New rate = $(2)[\text{N}_2] \times (3[\text{H}_2])^3 = 2 \times 27 = 54$ times
- 76.(b)** $2(+1) + 2x + 7(-2) = 0$, where x is oxidation state of Cr
 $2 + 2x - 14 = 0$, therefore $x = +6$
- 77.(d)** As positive charge increases, ionic radius decreases (a is correct). Down the group, ionic radius increases (c is correct).
- 78.(a)** Mn changes from +7 to +2, so electrons transferred = 5
 Equivalent weight = Molecular weight/5 = $158/5$
- 79.(c)** In ethyne, each carbon forms 2 sigma bonds and has 2 pi bonds, indicating sp hybridization.
- 80.(b)** Lucas reagent gives immediate turbidity with tertiary alcohols, turbidity after heating with secondary alcohols, and no reaction with primary alcohols.
- 81.(b)** C_4H_{10} can exist as n-butane ($\text{CH}_3 - \text{CH}_2 - \text{CH}_2 - \text{CH}_3$) and isobutane ($\text{CH}_3 - \text{CH}(\text{CH}_3) - \text{CH}_3$)
- 82.(a)** Here $g(x) = \log_e(x + \sqrt{x^2 + 1})$
 $g(-x) = \log_e(-x + \sqrt{x^2 + 1}) = -\log_e(x + \sqrt{x^2 + 1}) = -g(x)$
 So $g(x)$ is odd. Also sine is odd. So their composition is odd.
- 83.(d)** Given $\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \frac{1}{4^4} + \frac{1}{5^4} + \frac{1}{6^4} + \dots$ to $\infty = \frac{\pi^4}{90}$
- or, $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots + \left(\frac{1}{2^4} + \frac{1}{4^4} + \frac{1}{6^4} + \dots \right) = \frac{\pi^4}{90}$
 or, $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots + \left(\frac{1}{2^4} + \frac{1}{2^4} + \frac{1}{2^4} + \dots \right) = \frac{\pi^4}{90}$

$$= \frac{\pi^4}{90}$$

 or, $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots + \frac{1}{2^4} \left(\frac{1}{1^4} + \frac{1}{2^4} + \frac{1}{3^4} + \dots \right) = \frac{\pi^4}{90}$
 or, $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots + \frac{1}{16} \frac{\pi^4}{90} = \frac{\pi^4}{90}$
 or, $\frac{1}{1^4} + \frac{1}{3^4} + \frac{1}{5^4} + \dots = \frac{\pi^4}{90} - \frac{1}{16} \frac{\pi^4}{90} = \frac{15}{16} \frac{\pi^4}{90}$

$$= \frac{\pi^4}{96}$$
- 84.(b)** Given $\left(\frac{1-i}{1+i} \right)^{100} = a + ib$
 or, $\left(\frac{1-i}{1+i} \times \frac{1-i}{1-i} \right)^{100} = a + ib$
 or, $\left(\frac{1-2i+i^2}{1^2-i^2} \right)^{100} = a + ib$
 or, $\left(\frac{1-2i-1}{1+1} \right)^{100} = a + ib$
 or, $\left(\frac{-2i}{2} \right)^{100} = a + ib$
 or, $(-i)^{100} = a + ib$
 $(i^4)^{25} = a + ib$
 or, $1 = a + ib$
 or, $1 + 0i = a + ib$
 $\Rightarrow a = 1, b = 0$
- 85.(c)** Given $\begin{vmatrix} a & 1 & a+c \\ b & 1 & c+a \\ c & 1 & a+b \end{vmatrix}$
 Applying $C_3 \rightarrow C_3 + C_1$, $\begin{vmatrix} a & 1 & a+b+c \\ b & 1 & a+b+c \\ c & 1 & a+b+c \end{vmatrix}$

$$= (a+b+c) \begin{vmatrix} a & 1 & 1 \\ b & 1 & 1 \\ c & 1 & 1 \end{vmatrix} = 0 \quad (\because C_2 = C_3)$$
- 86.(b)** $C(n, 2) = 28$
 or, $\frac{n!}{(n-2)! 2!} = 28$
 or, $\frac{n(n-1)(n-2)!}{(n-2)! 2!} = 28$
 or, $x^2 - n - 56 = 0$
 or, $(n-8)(n+7) = 0$
 $\therefore n = 8$
- 87.(b)** Given $(1+x^2)^{40} \left(x^2 + 2 + \frac{1}{x^2} \right)^{-5}$

$$= (1+x^2)^{40} \left\{ \left(x + \frac{1}{x} \right)^2 \right\}^{-5}$$

$$= (1+x^2)^{40} \left(\frac{1+x^2}{x} \right)^{-10}$$

$$= (1+x^2)^{40} \frac{(1+x^2)^{-10}}{x^{-10}} = (1+x^2)^{30} x^{10}$$

 So, coefficient of x^{20} in $(1+x^2)^{30} x^{10}$

$$= \text{Coefficient of } x^{10} \text{ in } (1+x^2)^{30}$$

$$= C(30, 5) \text{ or } C(30, 25)$$

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88.(b) Let $y = m_1x$ and $y = m_2x$ be the lines represented by $x^2 + \lambda xy - 3y^2 = 0$. Then $m_1 + m_2 = \frac{\lambda}{-3}$, $m_1m_2 = \frac{1}{-3}$

Here, $m_1 + m_2 = 2m_1m_2$

$$\text{or, } -\frac{\lambda}{3} = 2 \times \frac{1}{-3}$$

$$\Rightarrow \lambda = 2$$

89.(c) Eccentricity of hyperbola

$$= \sqrt{1 + \frac{81}{144}} = \sqrt{\frac{225}{144}} = \frac{15}{12} = \frac{5}{4}$$

$$\text{and foci} = (\pm ae, 0) = \left(\pm \frac{12}{5} \times \frac{5}{4}, 0\right) = (\pm 3, 0)$$

Again foci of ellipse $= (\pm ae, 0) = (\pm \sqrt{16 - b^2}, 0)$

$$\text{So, } \sqrt{16 - b^2} = 3 \Rightarrow 16 - b^2 = 9 \Rightarrow b^2 = 7$$

90.(b) $|\vec{a} \times \vec{i}|^2 + |\vec{a}|^2 |\vec{i}|^2 \sin^2 \alpha = |\vec{a}|^2 \sin^2 \alpha$

$$|\vec{a} \times \vec{i}|^2 = |\vec{a}|^2 \sin^2 \alpha$$

$$|\vec{a} \times \vec{j}|^2 = |\vec{a}|^2 \sin^2 \beta$$

$$|\vec{a} \times \vec{k}|^2 = |\vec{a}|^2 \sin^2 \gamma$$

$$\text{So, } |\vec{a} \times \vec{i}|^2 + |\vec{a} \times \vec{j}|^2 + |\vec{a} \times \vec{k}|^2$$

$$= |\vec{a}|^2 (\sin^2 \alpha + \sin^2 \beta + \sin^2 \gamma) = 2|\vec{a}|^2$$

[Note that line makes angles α, β, γ with the coordinate axes].

91.(d) Given $\cos^{-1}\sqrt{p} + \cos^{-1}\sqrt{1-p} + \cos^{-1}\sqrt{1-q} = \frac{3\pi}{4}$

$$\text{or, } \cos^{-1}\sqrt{p} + \sin^{-1}\sqrt{p} + \cos^{-1}\sqrt{1-q} = \frac{3\pi}{4}$$

$$\text{or, } \cos^{-1}\sqrt{1-q} = \frac{\pi}{4}$$

$$\text{or, } \sqrt{1-q} = \cos \frac{\pi}{4}$$

$$\Rightarrow \sqrt{1-q} = \frac{1}{\sqrt{2}}$$

$$\Rightarrow 1-q = \frac{1}{2} \Rightarrow q = \frac{1}{2}$$

92.(c) Given $f(x) = x^n$, $f'(x) = nx^{n-1}$, $f''(x) = n(n-1)x^{n-2}$, ..., $f^{(n)}(x) = n(n-1)(n-2) \dots 1 = n!$

$$\text{Now, } f(1) - \frac{f'(1)}{1!} + \frac{f''(1)}{2!} - \dots + \frac{(-1)^n f^{(n)}(1)}{n!}$$

$$= 1 - \frac{n}{1!} + \frac{n(n-1)}{2!} - \dots + (-1)^n \frac{n!}{n!}$$

$$= C(n, 0) - C(n, 1) + C(n, 2) - \dots + (-1)^n C(n, n)$$

$$= (1-1)^n = 0$$

93.(a) Given, $y^2 = 5x - 1$

$$\text{or, } \frac{dy^2}{dy} \frac{dy}{dx} = 5 \frac{dx}{dx} - \frac{d}{dx}$$

$$\text{or, } 2y \frac{dy}{dx} = 5$$

$$\text{or, } \frac{dy}{dx} = \frac{5}{2y}$$

$$\text{At point } (1, -2), \text{ slope of tangent} = \frac{5}{2(-2)} = -\frac{5}{4}$$

$$\text{So, slope of normal} = \frac{4}{5}$$

Normal is $ax - 5y + b = 0$

$$\text{So, slope} = -\frac{a}{-5}$$

$$\text{or, } \frac{4}{5} = \frac{a}{5}$$

$$\text{i.e. } a = 4$$

$$\text{Also, } 4 \times 1 - 5(-2) + b = 0$$

$$4 + 10 + b = 0$$

$$\text{i.e. } b = -14$$

94.(b)

$$I = \int \frac{x \sin^{-1} x}{\sqrt{1-x^2}} dx$$

$$\text{Put } y = \sin^{-1} x$$

$$\therefore dy = \frac{1}{\sqrt{1-x^2}} dx$$

$$\text{Then } I = \int y \sin y dy$$

$$= y \int \sin y dy - \int \left(\frac{dy}{dx} \int \sin y dy \right) dy$$

$$= -y \cos y - \int -\cos y dy$$

$$= -y \cos y + \sin y + c = -\sin^{-1} x \sqrt{1-x^2} + x + c$$

95.(b)

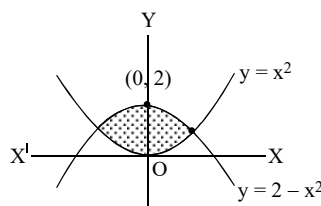
$$\int_{-1}^3 \left[\tan^{-1} \frac{x}{x^2+1} + \tan^{-1} \frac{x^2+1}{x} \right] dx$$

$$= \int_{-1}^3 \left[\tan^{-1} \frac{x}{x^2+1} + \tan^{-1} \frac{x}{x^2+1} \right] dx$$

$$= \int_{-1}^3 \frac{\pi}{2} dx = \frac{\pi}{2} \int_{-1}^3 dx = \frac{\pi}{2} [x]_{-1}^3 = \frac{\pi}{2} [3 - (-1)]$$

$$= \frac{\pi}{2} \times 4 = 2\pi$$

96.(a)



Given curves are

$$y = x^2 \dots (i) \quad y = 2 - x^2 \dots (ii)$$

Solving (i) and (ii),

$$x^2 = 2 - x^2$$

$$\text{or, } 2x^2 = 2 \quad \text{or, } x^2 = 1 \quad \text{i.e., } x = \pm 1$$

Thus the required area

$$= 2 \int_{-1}^1 (y_1 - y_2) dx$$

$$= 2 \int_{-1}^1 (2 - x^2 - x^2) dx$$

$$= 2 \int_{-1}^1 (2 - 2x^2) dx$$

$$= 4 \int_{-1}^1 (1 - x^2) dx$$

$$= 4 \left[x - \frac{x^3}{3} \right]_{-1}^1 = 4 \left(1 - \frac{1}{3} \right) - 0$$

$$= 4 \times \frac{2}{3} = \frac{8}{3} \text{ sq. units}$$

97.(c)

98.(b)

99.(b)

100.(c)

...Best of Luck...